Propagation of tectonic waves

Laurent Husson, MIT (lhusson@mit.edu) Yanick Ricard, Yale / ENS-Lyon (ricard@ens-lyon.fr)

1) Crust stability vs lithosphere instability

Crustal deformation results from the disequilibrium between boundary stresses and buoyancy stresses arising from lateral density variations within the lithosphere. The positive buoyancy of the light crust with respect to the underlying mantle induces a tendency to collapse (a_c). The cool and dense thermal boundary layer forming the lithospheric mantle has a negative buoyancy which tends to generate Rayleigh-Taylor instabilities in the lithosphere (a_{θ}). Here we show that an alternative domain in which deformation is propagated laterally dominates in continents.

Stress balance :
$$4L_0 \frac{\partial}{\partial x} \eta \frac{\partial u}{\partial x} = \frac{\partial M}{\partial x}$$
, M is the moment of the lithospheric mass anomalies $M = \int_0^{+\infty} \delta \rho g z \, dz$ MomentsCrustal : $M_c = \frac{1}{2}\rho_c g(1 - \frac{\rho_c}{\rho_m})S^2$
Thermal : $M_{\theta} = -\frac{1}{3}\rho_m \alpha \Delta \theta g L^2$ Elevation : $h = \frac{\rho_m - \rho_c}{\rho_m}S - \frac{1}{2}\alpha \Delta \theta L$ Transportmass conservation : $\frac{\partial M_c}{\partial t} + u \frac{\partial M_c}{\partial x} + 2M_c \frac{\partial u}{\partial x} = 0$
heat conservation : $\frac{\partial M_{\theta}}{\partial t} + u \frac{\partial M_{\theta}}{\partial x} + 2M_{\theta} \frac{\partial u}{\partial x} = \kappa \frac{\partial^2 M_{\theta}}{\partial x^2}$

ac: transport of the crustal moment $a\theta$: transport of the mineralogical mantle moment b: lateral diffusion of the thermal moment g: gravitational acceleration S: crustal thickness h: elevation $\rho_{\rm C}$: crustal density ρ_m: asthenospheric mantle density ρ_{θ} : lithospheric mantle density

 $\Delta \theta$: temperature increase across the lithosphere



2) Stability analysis



Let's assume that the solution is a uniform state + infinitesimal perturbations. In dimensionless form : $\tilde{M}_c = M_c^0 + \epsilon m_c(x, t)$

 $\tilde{M}_{\theta} = M_{\theta}^{0} + \epsilon m_{\theta}(x, t)$ $\tilde{u} = \epsilon u(x, t)$

Assuming that all terms of order ε go as exp(ikx + σt), we show from the above equations that : $2\sigma^{2} + \sigma(M_{\theta}^{0} + M_{c}^{0} + 2k^{2}) + k^{2}M_{c}^{0} = 0$

$$k_1 = \frac{(\sqrt{|M_{\theta}^0|} - \sqrt{M_c^0})}{\sqrt{2}} \quad k_2 = \frac{(\sqrt{|M_{\theta}^0|} + \sqrt{M_c^0})}{\sqrt{2}}$$

* If 0 < k < |k1| or k > k2, the roots are real :

$$\sigma = \frac{1}{2}(k_1k_2 - k^2) \pm \frac{1}{2}\sqrt{(k_1^2 - k^2)(k_2^2 - k^2)}$$

* If |k1| < k < k2, the roots are imaginary ($\sigma = Real(\sigma)$) $+i\omega$):

 $Real(\sigma) = \frac{1}{2}(k_1k_2 - k^2) \qquad \omega = \frac{1}{2}\sqrt{(k^2 - k_1^2)(k_2^2 - k^2)}$

A propagating mode develops with phase velocity ω /k and group velocity $d\omega/dk$.

And if $\text{Real}(\sigma) = 0$, the system undergoes a pure propagating mode, with :

$$k_0 = \sqrt{k_1 k_2}$$
, and $\omega = \frac{1}{2} k_0 (k_2 - k_1)$

and propagates with a group velocity (= wave velocity):

 $\left(\kappa\rho_{c}(\rho_{m}-\rho_{c})g\right)_{S}$ (real units)

3) Non-linear solutions

A full solution of our set of equations can be calculated to test the validity of the results of the stability analysis. Three situations arise :

(a) The crust dominates the system which restores uniform thicknesses. Boring ! (b) The lithosphere dominates : the instability rapidly destabilizes the whole system and becomes a regular Rayleigh-Taylor instability.

(c) The system is in the propagating mode. In the unstable domain (c1), the asymetric development of the instabilities resembles a series of subductions. In the purely propagating case, the waves propagate indefinitely. In the propagating mode, the thickness variations are out of phase (d).





1st stage

mountain belt

plateau develop

4th stage

collapse

The thickness variations of the lithosphere are in advance to those of the crust, in the direction of propagation. They induce compression and thus thickening on the right hand side of the mountain range that collapses on the left hand side.



Group Velocity

 lk_1

-2



hortening

EC

SAZ

With S=40 km, L=83 km, η =2 10²¹ Pa s, L0=50 km, propagation occurs for wavelengths between 26 km and 3140 km, i.e. most of continental tectonics are in the propagating mode. Typical values for velocity are 3.2 to 6.4 mm yr⁻¹. Constant amplitude propagation occurs for k0=287 km at v_p =3.7 mm yr⁻¹.

^(m) after Baumont et al, 01

WC





The tectonic evolution of high plateaus can be summarized in a 4 stage development sketch. Each stage currently exists on Earth : subduction i) gaussian mountain belt : compression (*e.g.* Southern Andes). = wave nursery ii) short plateau : stresses are neutral next to the subduction, compressive hinterland (e.g. Central Andes).

iii) wider plateau : extension next to the the subduction, compression hinterland (e.g. Tibet).

iv) collapse : extension everywhere (*e.g.* W. Cordilleras).

Tectonic waves transfer deformation away from subduction zones. Our model (A) shows the evolution of a lithosphere submitted to a interplate traction Σ (model recycled from Husson & Ricard, 2004 now including) lithospheric instabilities). This model is compatible with tomographic observations (Andes, Tibet) and stress data.

Note that this model of high plateaus is in the stable propagating mode but the ratio of initial moments can also lead to destabilization hinterland or even pure steady state propagation.

Cosmetic improvements (B, viscosity increases hinterland) generate even better plateau shape.



Another application of this propagative mode could be the self activation of rifts.

England, P. and D. McKenzie. A thin viscous sheet model for continental deformation, Geophys. J. R. Astron. Soc., 70, 295-321, 1982.

Houseman, G.A., D.P. McKenzie and P. Molnar. Convective instability of a thickened boundary layer and its relevance for the thermal evolution of continental convergent belts. J. Geophys. Res., 86, 6115--6132, 1981.

- Husson, L. and Y. Ricard. Stress balance above subduction zones: application to the Andes. Earth Planet. Sci. Lett., 222, 1037-1050, 2004.
- Neil, E.A. and G.A. Houseman. Rayleigh-Taylor instability of the upper mantle and its role in intraplate orogeny, Geophys. J. Int., 138, 89-107, 1999.

Lemery, C., Y. Ricard and J. Sommeria. A model for the emergence of thermal plumes in Rayleigh-B'enard convection and infinite Prandtl number. J. Fluid Mech., 414, 225-250, 2000.

Ricard, Y. and L. Husson. Propagation of tectonic waves. Geoph. Res. Lett., in press.