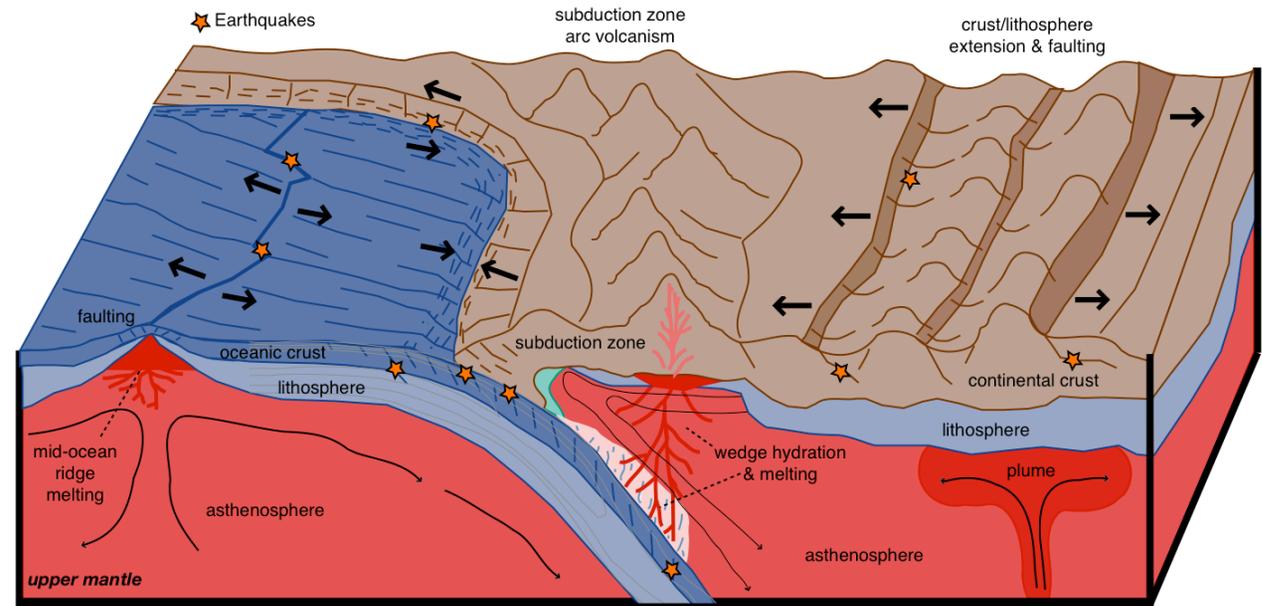
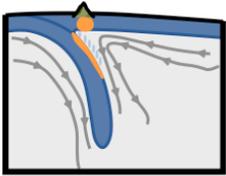


Subduction Zone & Slab Processes

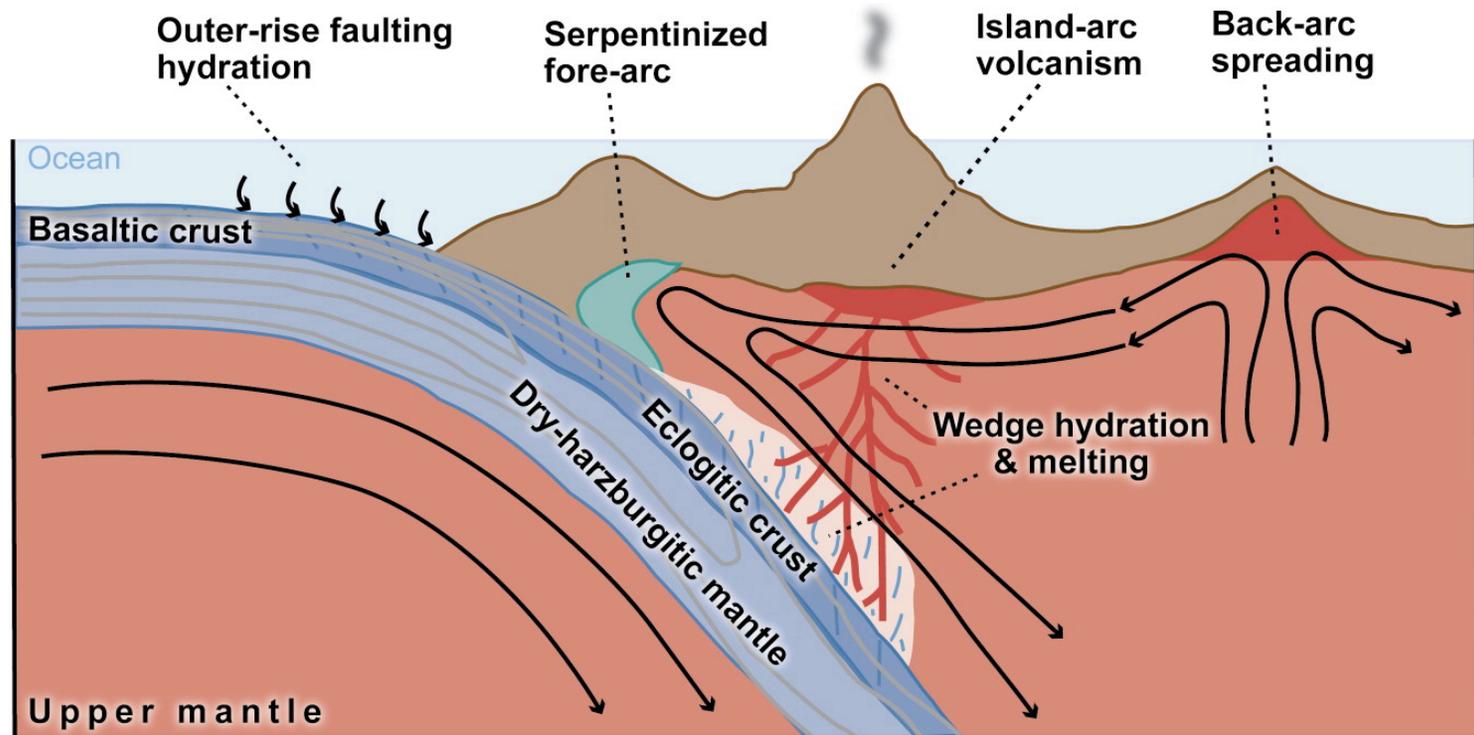
**11th International
Workshop on
Modeling
of Mantle
Convection
& Lithospheric
Dynamics
Braunwald,
Switzerland**



***Magali Billen
Department of Geology
U.C. Davis***

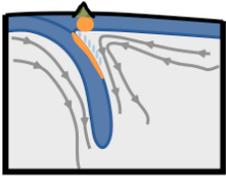


Regional View of the SZ



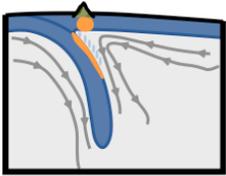
 Billen MI. 2008.
Annu. Rev. Earth Planet. Sci. 36:325–56.

- *How did we get to this picture?*
- *What are we still missing?*



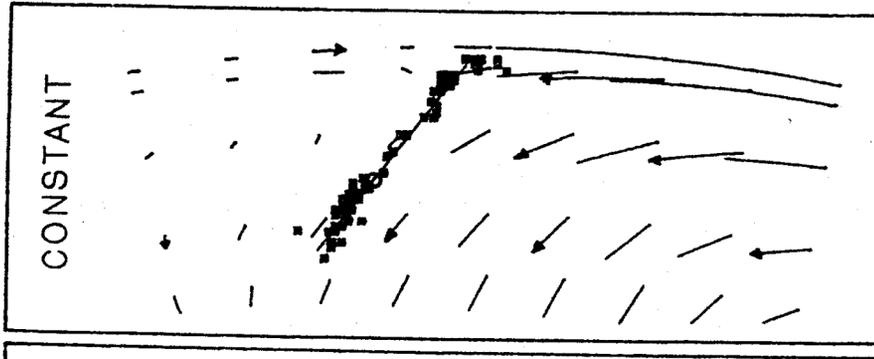
More Questions than Answers

- Some slabs appear to subduct into the deep lower mantle, while others get stuck in the transition zone and mid-mantle: why is it that, so far, only physical models with an unrealistically large clapeyron slope for the 660-km phase change and weak slabs can **trap slabs** in the mid-mantle?
- Rheological constraints predict that slabs should deform plastically at **high effective viscosities**: why are physical models with weak or moderately-strong slabs successful?
- Geological observations of surface deformation call for long-term coupling between overriding and subducting plates: why are models without an **overriding plate** successful?
- Rheological and seismological constraints predict that the upper mantle deforms by dislocation creep (**non-Newtonian rheology**): why are Newtonian models of slab dynamics successful?
- Tomographic images of slabs in the deep mantle imply significant **thickening of slabs** (5-10 x): why are most physically-modelled slabs so thin (1.5-2.0 x)?

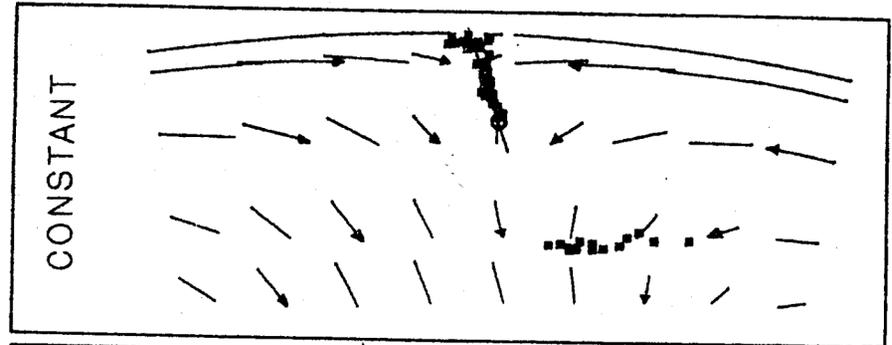


Why so many Questions?

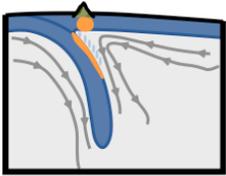
TONGA



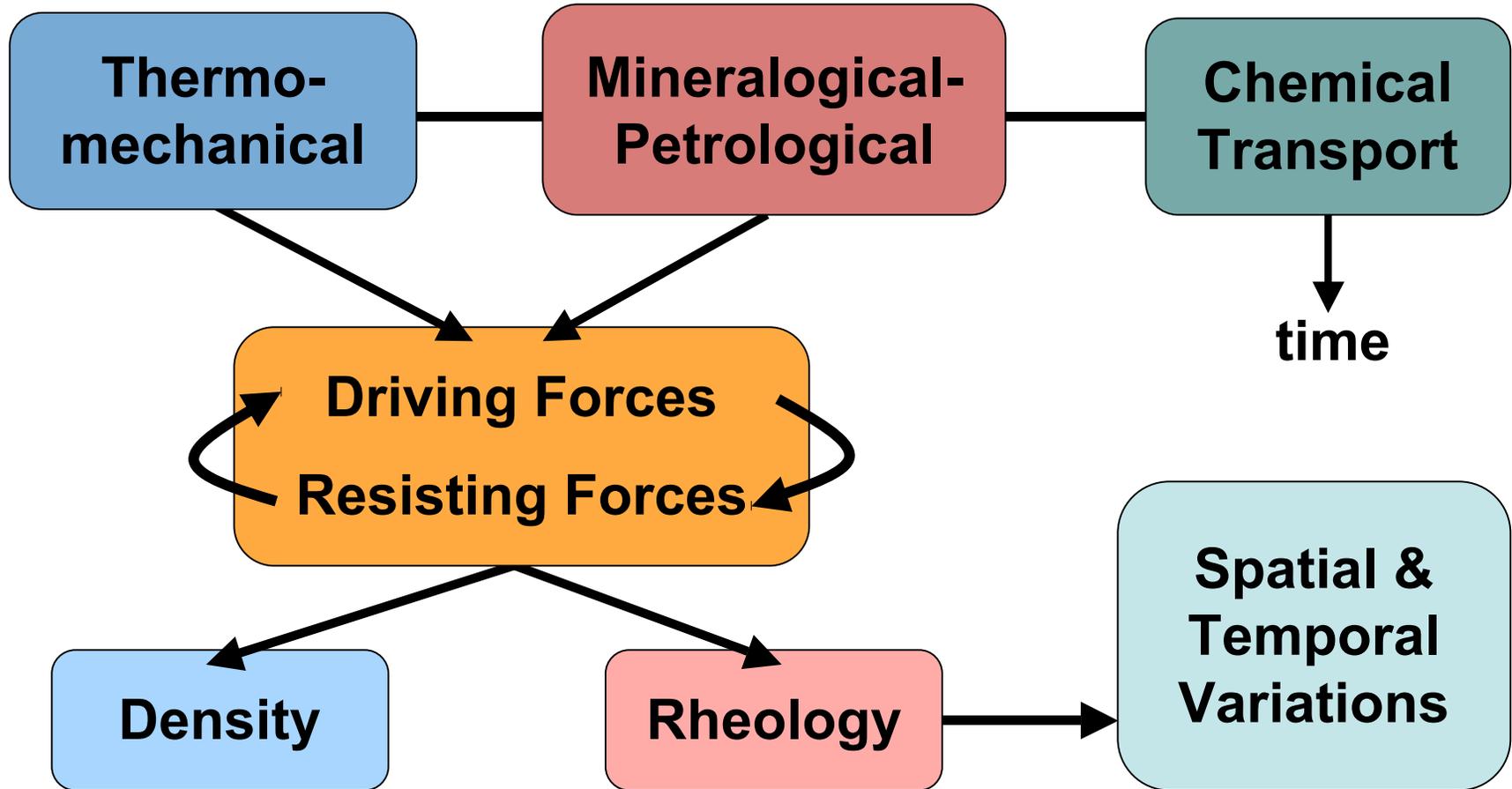
NEW HEBRIDES



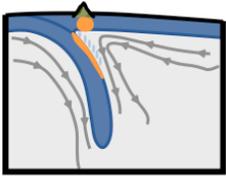
We know something is missing, but we still match observations.



The Dynamical System

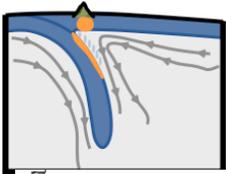


- **Non-linear interactions & dynamic feed-backs.**

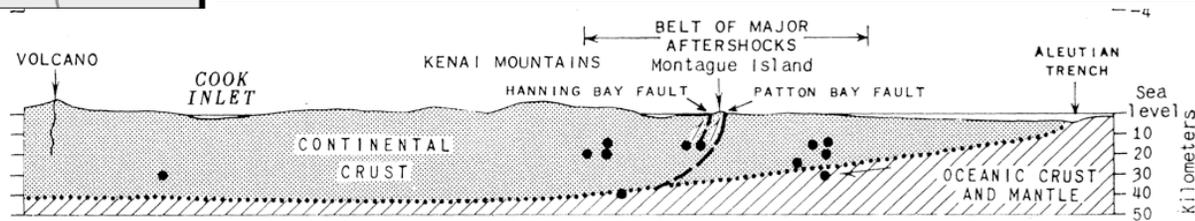


Outline

- **Historical Perspective**
 - **Pre**-Plate Tectonics
 - **Since** Plate Tectonics
 - An **Unprecedented** Time for Subduction Models
- **The Dynamical System**
 - Thermo-mechanical: driving & resisting forces.
 - Mineralogical-petrological: linking to **fluids**.
 - Chemical Transport - **the importance of time**.
- **Conclusions**
 - Transforming a kinematic theory of plate tectonics to a dynamic theory.



Pre - Plate Tectonics

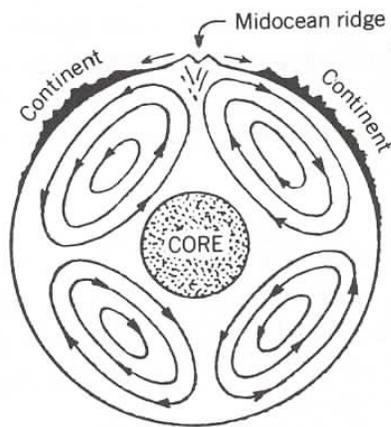


Internal deformation of subducted lithosphere.
- Isacks & Molnar, 1969

Deep planar fault zone
- Elsasser, 1968

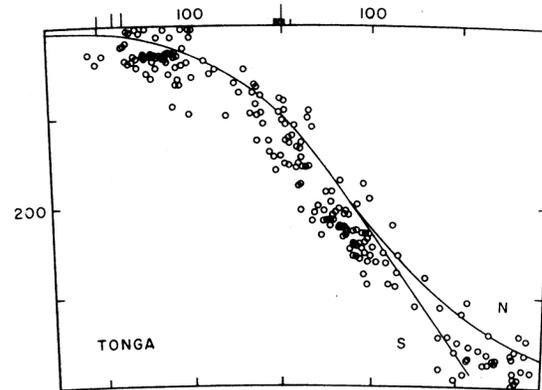
Lithospheric thrusting
- Plafker, 1965

Crustal-scale thrusting
- Hess, 1962



Mantle Convection
- Holmes, 1944

1940s



Mega-shear to 700 km
- Benioff, 1954

1950s

1960s

- **Subduction into the mantle was one of the last pieces of the plate tectonics puzzle.**

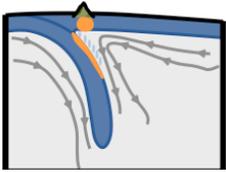
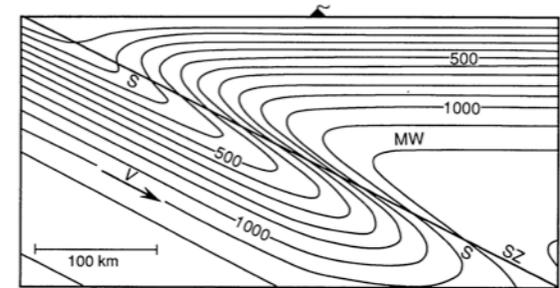
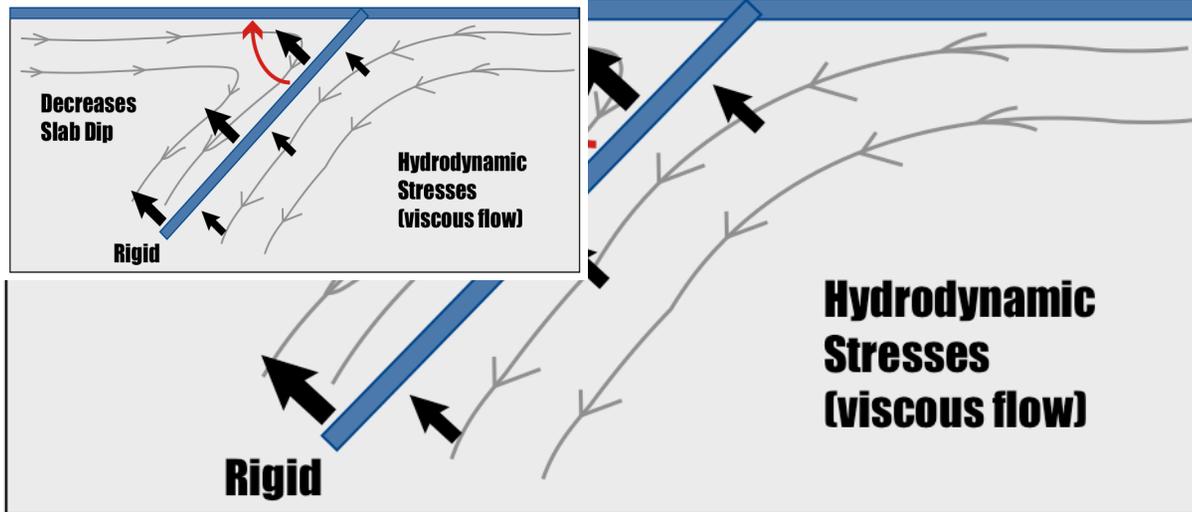


Plate Tectonics: in the SZ



Linking slab temp. to mineralogy & petrology
- Peacock, 1990

Slab thermal structure
- Toksov, 1971; 1973

Corner-flow model.
- McKenzie, 1969

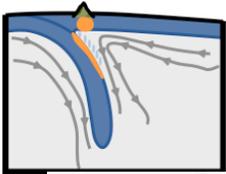
Dynamic topography from corner-flow
- Sleep, 1975

1960s

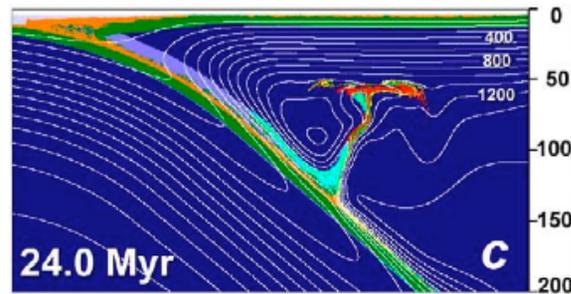
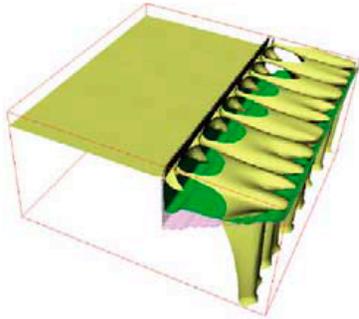
1970s → 1980s

1970s → 1990s

- **Early analytic models capture major processes.**
 - Force balance on slab.
 - Slab thermal structure.



Kinematic Slab - Dynamic Wedge



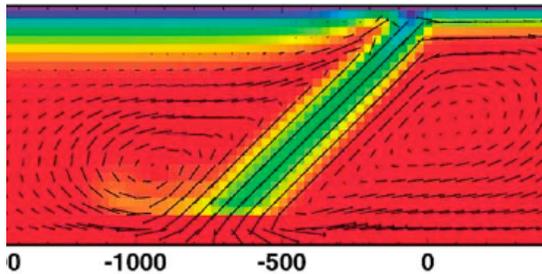
3D, anisotropy implication
- Kneller & van Keken, 2007

Non-linear viscosity
- Kneller et al., 2007

Compositional & phase:
density & viscosity
- Gerya & Yuen, 2003

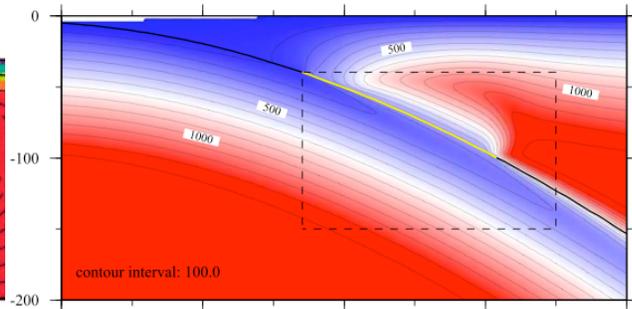
Low viscosity wedge
- Honda & Saito, 2003

Temperature-dep. visc.
- Eberle, 2001



Wedge/back arc flow

- Bodri & Bodri, 1978
- Toksov & Hsui, 1978



Convection in the wedge

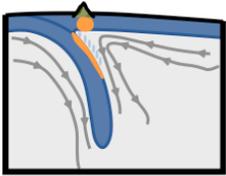
- Ida, 1983
- Honda, 1985

1970s

1980s

1990s → 2000s

- *Slab & mantle wedge thermal/min./pet. structure.*
- *Fluid transport*
- *Seismic anisotropy.*



Observations

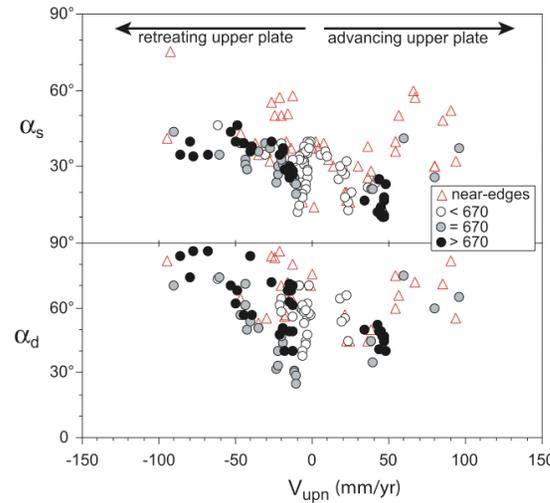
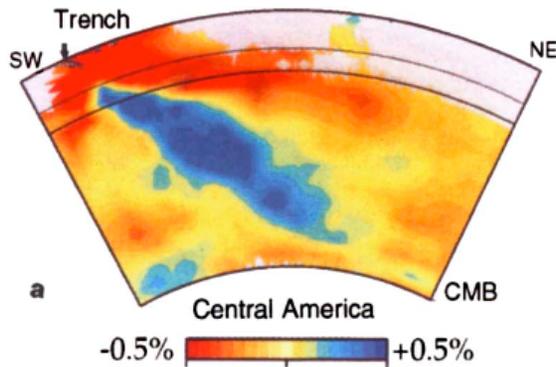


Plate kinematics & characteristics

- Mueller et al., 1997
- Lallemand et al., 2005

Seismic anisotropy

- Russo & Silver, 1994
- Fischer et al., 1998
- Long & Silver, 2008

Plate kinematics & characteristics

- Jarrard, 1986

Seismic tomography

- e.g., van der Hilst, 1997

Arc curvature, slab dip, subduction velocity.

- Tovish & Schubert, 1978

Geoid & dynamic topo.

- Hager 1984

Plate tectonic reconstructions.

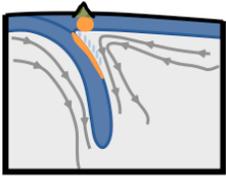
- e.g., DeMets, 1990

1970s

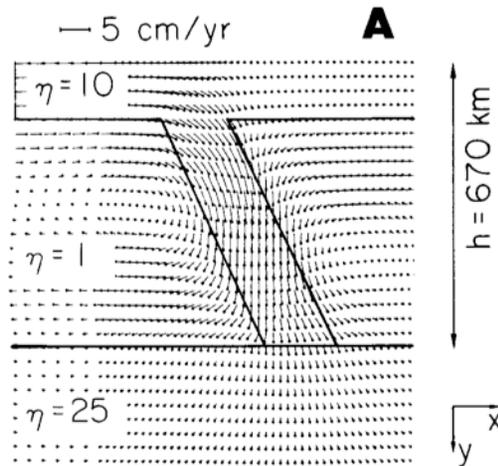
1980s

1990s → 2000s

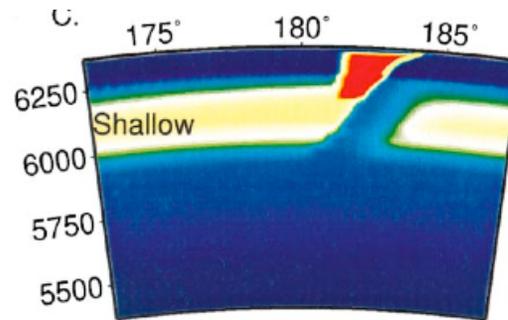
- **Connecting kinematics to dynamics.**



Instantaneous (quasi) Dynamic



Stress-state in slab
- Vassiliou, 1984



3D, Weak plate bndy, non-linear rheology
- Zhong & Gurnis, 1996
3D, Lateral (moderate) viscosity variations
- Moresi et al., 1996
2D, Faults & non-linear viscosity
- Zhong & Gurnis, 1992, 1994

2D, Overriding plate root geometry & slab suction

- Driscoll et al., 2009

3D, Slab strength effect toroidal & poloidal flow

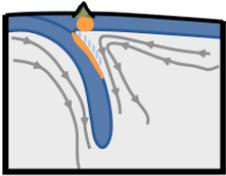
3D, Temp-dep, low viscosity wedge
- Billen & Gurnis, 2001

1980s

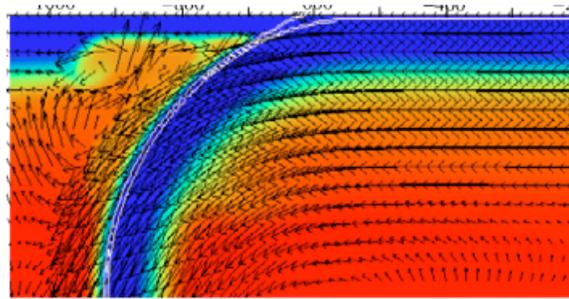
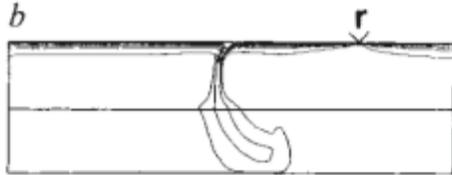
- **Rheologic Structure:**
 - mantle, slab, plate boundaries, wedge, crust...
- **Surface deformation:**
 - topography, geoid, stress-state.

1990s

2000s



Fully Dynamic (t-dependent)



2D, wedge rheology
- Arcay et al., 2008

3D, Slab width effects
- Stegman, 2006

2D, Slab detachment
- Gerya & Yuen, 2004

3D, Trench migration
- Funiciello et al., 2003

2D, Comp., grain-size-dep. slab visc
- Cizkova et al., 2002

2D, Oceanic plateaus
- van Hunen et al 2000

2D, Temp-dep,
- Gurnis & Hager 1988

2D, Phase trans. (mech)
- Christensen & Yuen, 1984

2D, Subduction initiation
- Toth & Gurnis, 1998

2D, Trench migration
- Olbertz et al., 1997
- Griffiths et al., 1995

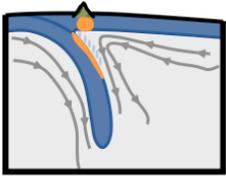
2D, Phase trans.
(T-dep. viscosity)
- King, 1991

1980s

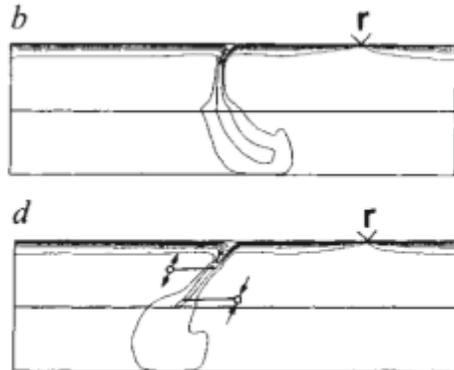
- *Buoyancy forces: phase transition, slab, crust...*
- *Rheologic structure: mantle, slab, wedge...*
- *Geometry: 2-D, 3-D, slab edges, interactions...*

1990s

2000s

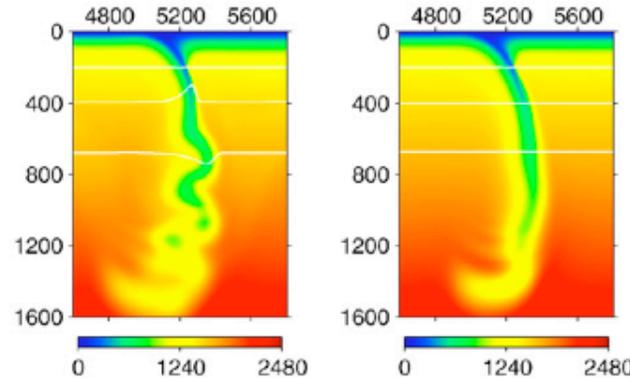


Fully Dynamic (t-dependent)



2D, Temp-dep,
- Gurnis & Hager 1988

2D, Phase trans. (mech)
- Christensen & Yuen, 1984



2D, Trench migration

- Olbertz et al., 1997
- Griffiths et al., 1995

2D, Phase trans.
(T-dep. viscosity)
- King, 1991

3D, Slab-edge flow & slab depth

- Honda, 2009

2D, Slab Buckling LM.
- Behoukova & Cizkova 2008

2D, Double-slab sub.
- Mishin et al., 2008

2D, 1-sided subduction
- Gerya et al., 2008

2D, Flat slabs & LVC
- Manea & Gurnis, 2007

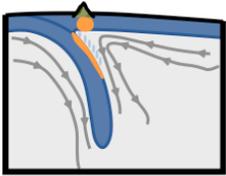
2D, wedge rheology
3D, Slab width effects
2D, Slab detachment
2D, Slab detachment
3D, trench migration
- Funicello et al., 2003
2D, Grain size dep. slab visc
- Van Hunen et al. 2000

1980s

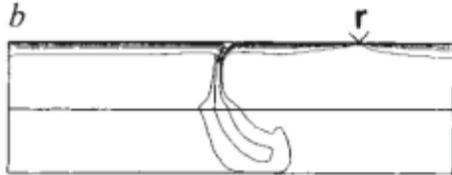
1990s

2000s

- *Buoyancy forces: phase transition, slab, crust...*
- *Rheologic structure: mantle, slab, wedge...*
- *Geometry: 2-D, 3-D, slab edges, interactions...*



Fully Dynamic (t-dependent)



2D, Compressibility
- Lee & King, 2009

2D, Meta-stable olivine,
- Schmeling, 1999

2D, Ridge-trench int.
- Burkett & Andrews, 2009

2D, Subduction initiation
- Toth & Gurnis, 1998

2D, Coupled/uncoupled
continental collision
- Faccenda et al., 2009

2D, Trench migration
- Olbertz et al., 1997
- Griffiths et al., 1995

3D, Slab-edge flow & slab depth
2D, Slab Sucking LM.
2D, Double slab subduction
2D, Irregular subduction
2D, Flat slabs & LVC
- Manea & Gurnis, 2007

2D, Temp-dep,
- Gurnis & Hager 1988

2D, Phase trans. (mech)
- Christensen & Yuen, 1984

2D, Phase trans.
(T-dep. viscosity)
- King, 1991

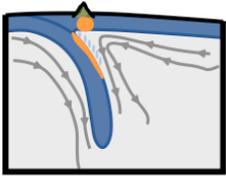
2D, wedge rheology
3D, Slab width effects
2D, Slab detachment
3D, trench migration
- Funicello et al., 2003
2D, Oceanic plateaus
- van Hunen et al. 2000

1980s

1990s

2000s

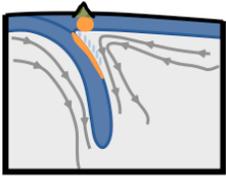
- *Buoyancy forces: phase transition, slab, crust...*
- *Rheologic structure: mantle, slab, wedge...*
- *Geometry: 2-D, 3-D, slab edges, interactions...*



A Multi-variate System

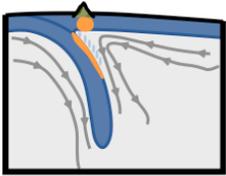
- **Geometrical Variables**
 - 2D vs. 3D
 - Over-riding plate
 - Interaction w/ other plate boundaries.
- **Mineral-/Petro-logical**
 - Compositional variation
 - Density
 - Rheology
- **Physical Properties**
 - Rheology
 - Thermal parameters (α, κ)
 - Compressibility
- **Coupled Systems**
 - Solid phase changes
 - Hydration/dehydration
 - Melting

Link to Observations & Time Evolution
Transform a kinematic theory to a dynamic theory.

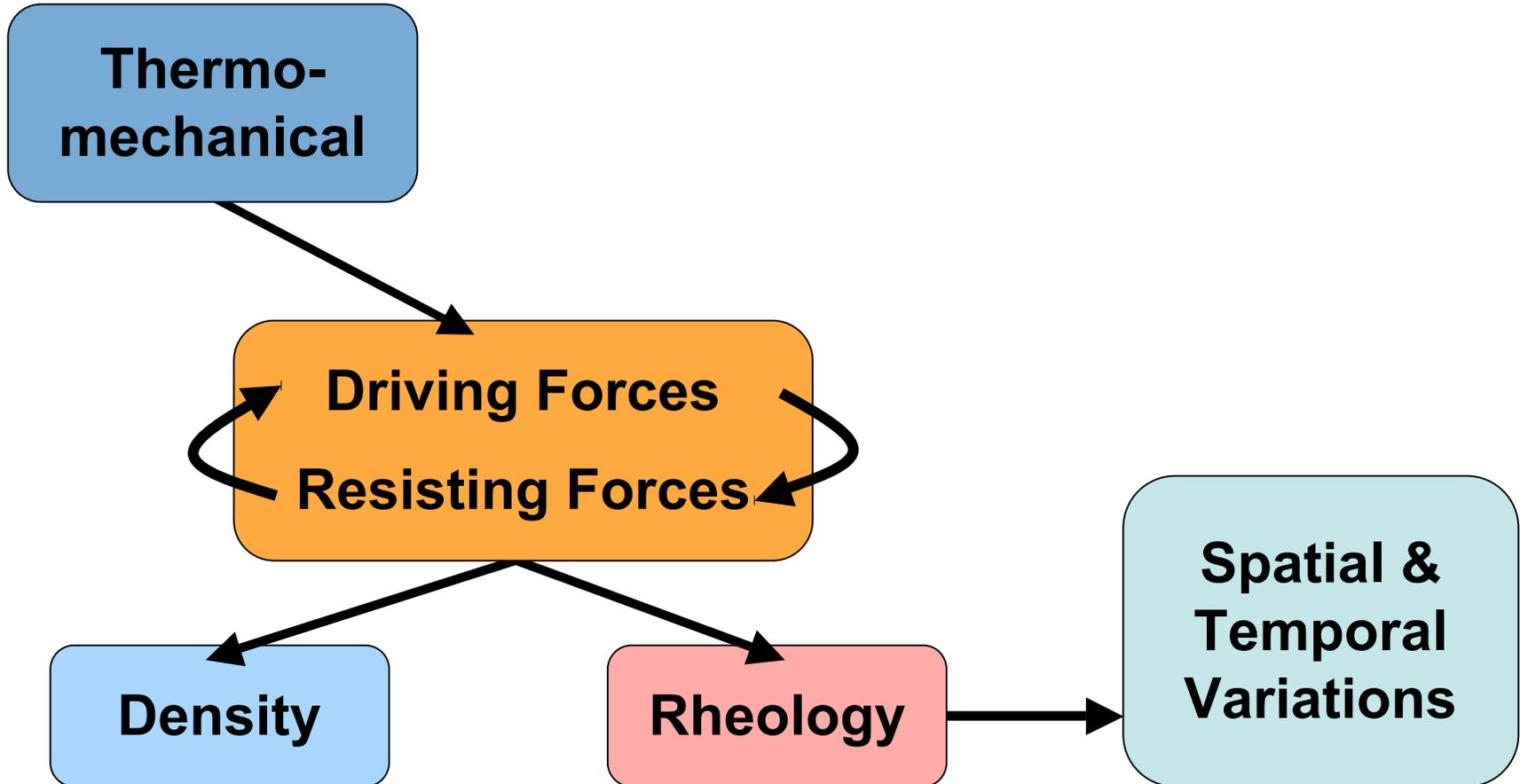


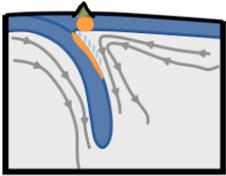
An *Unprecedented* Time

- **Access** to new & more complete observations on kinematics & geometry
 - plate tectonic reconstructions, seismic observations on slab shape, seismic anisotropy constraints on flow patterns.
- **Advances** in numerical & analogue methods
 - CPU-speed, RAM, parallel processing, better solvers; imaging techniques, materials...
- **Ability** to link dynamics to observations/ data/ processes from other disciplines
 - petrology, geochemistry (origins, process/transport times), geology-structures, thermo-barometry.



The Dynamical System





Thermo-Mechanical

- **Conservation Equations**

- Conservation of Mass:

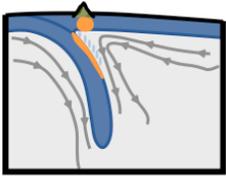
$$\frac{\partial \rho}{\partial t} + \nabla \cdot \rho \vec{v} = 0$$

- Conservation of Momentum:

$$\rho \left(\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \nabla) \vec{v} \right) = \nabla \cdot \vec{\sigma} - g \rho \vec{z}$$

- Conservation of Energy:

$$\frac{\partial C_p T}{\partial t} + \vec{v} \cdot \nabla C_p T = \frac{1}{\rho} \nabla \cdot k \nabla T + H$$



Thermo-Mechanical

- **Common simplifications.**

- Conservation of Mass (incompressible; $\delta\rho = 0$):

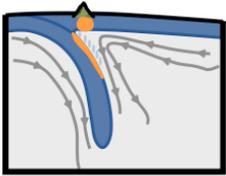
$$\nabla \cdot \vec{v} = 0$$

- *Compressibility: minor effects in shallow mantle (Lee & King, 2009).*
- Boussinesq Approximation ($\delta\rho \ll \rho$):

$$\rho = \rho_o(1 - \alpha(T - T_o))$$

- Constitutive Equation (incompressible):

$$\sigma_{ij} = \eta \left(\frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right) - p\delta_{ij}$$



Thermo-Mechanical

- **Simple Equations. Complexity comes from:**
 - **Geometry, material properties & variation in materials.**
 - Conservation of Mass (incompressible; $\delta\rho = 0$):

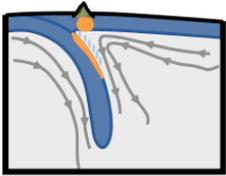
$$\nabla \cdot \vec{v} = 0$$

- Conservation of Momentum:

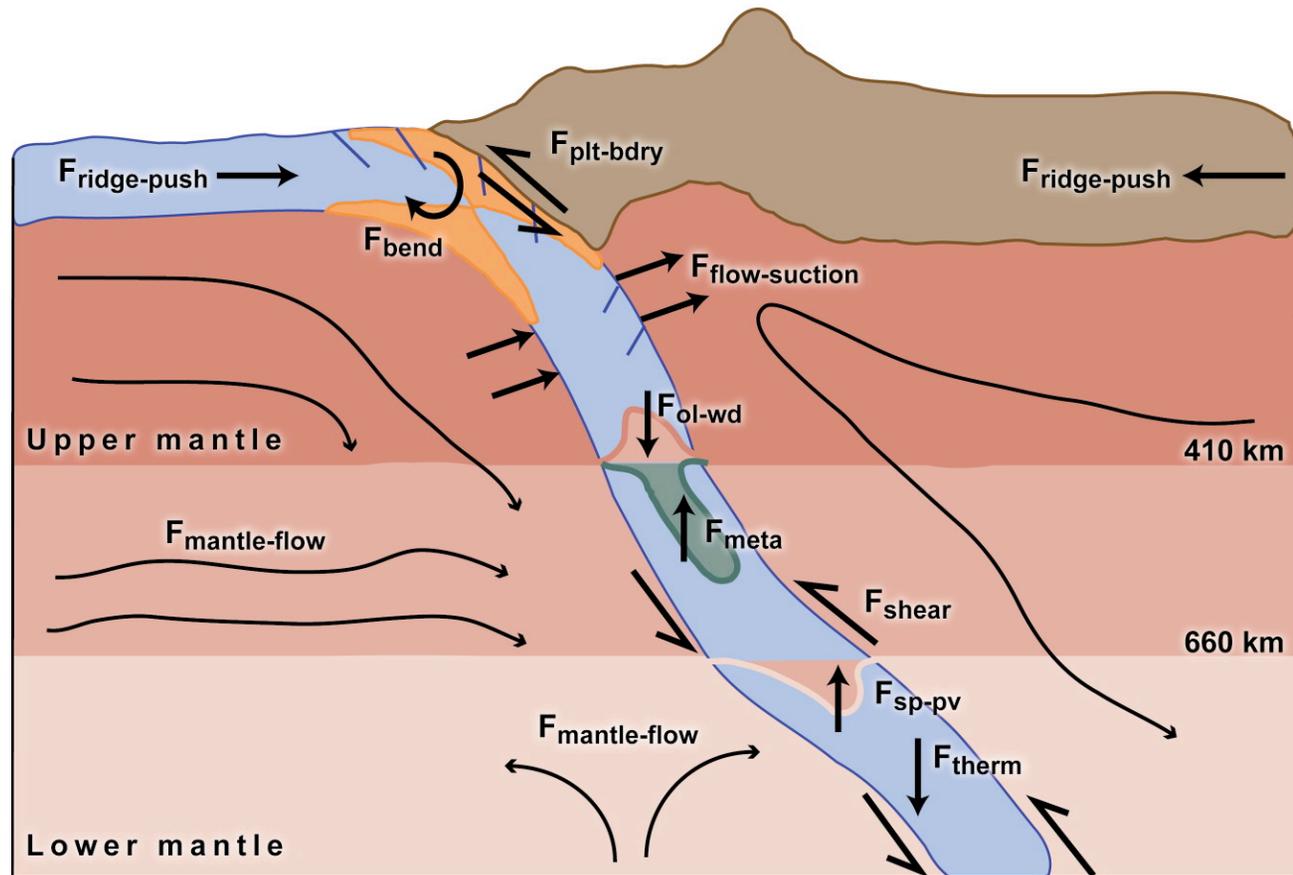
$$\rho \left(\frac{\partial \vec{v}}{\partial t} + (\vec{v} \cdot \nabla) \vec{v} \right) = \eta \nabla^2 \vec{v} - \nabla p - g\rho \vec{z}$$

- Conservation of Energy (constant C_p , κ ; $H = 0$):

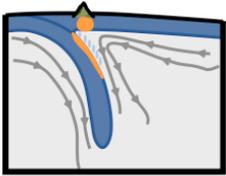
$$\rho \left(\frac{\partial T}{\partial t} + \vec{v} \cdot \nabla T \right) = \kappa \nabla^2 T + \frac{H}{C_p}$$



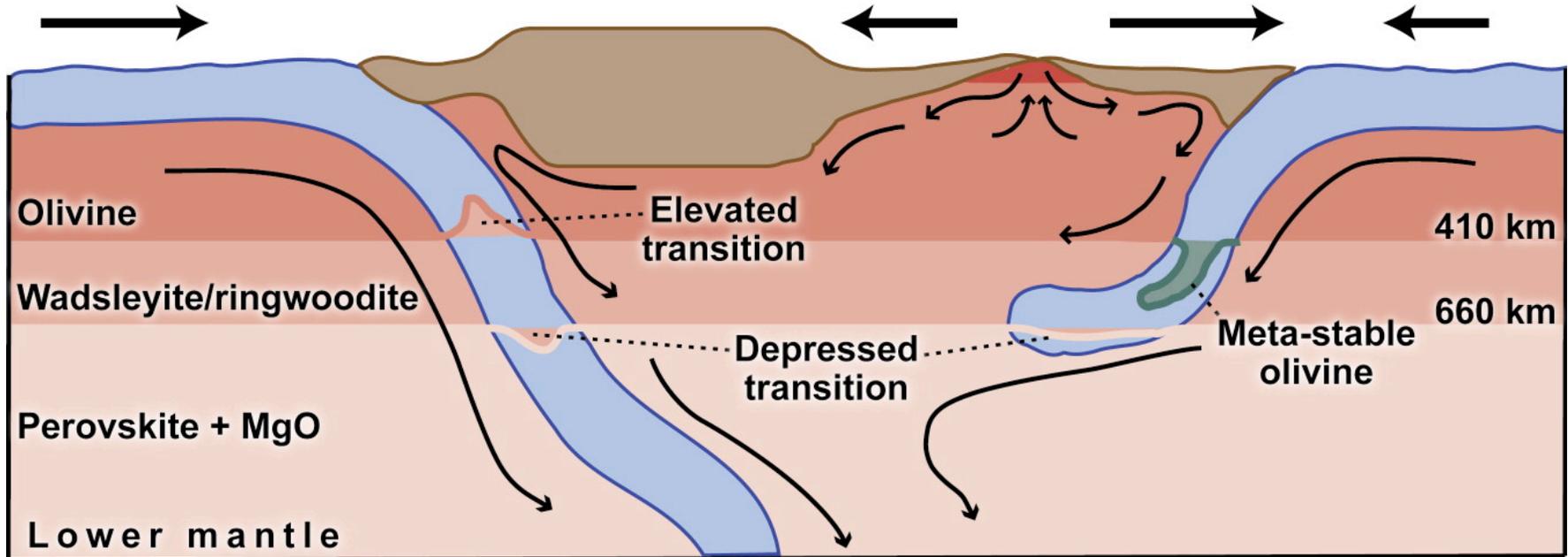
A Dynamic Slab



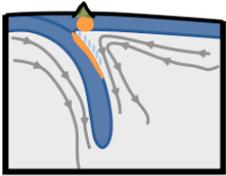
Driving forces vs. resisting forces...



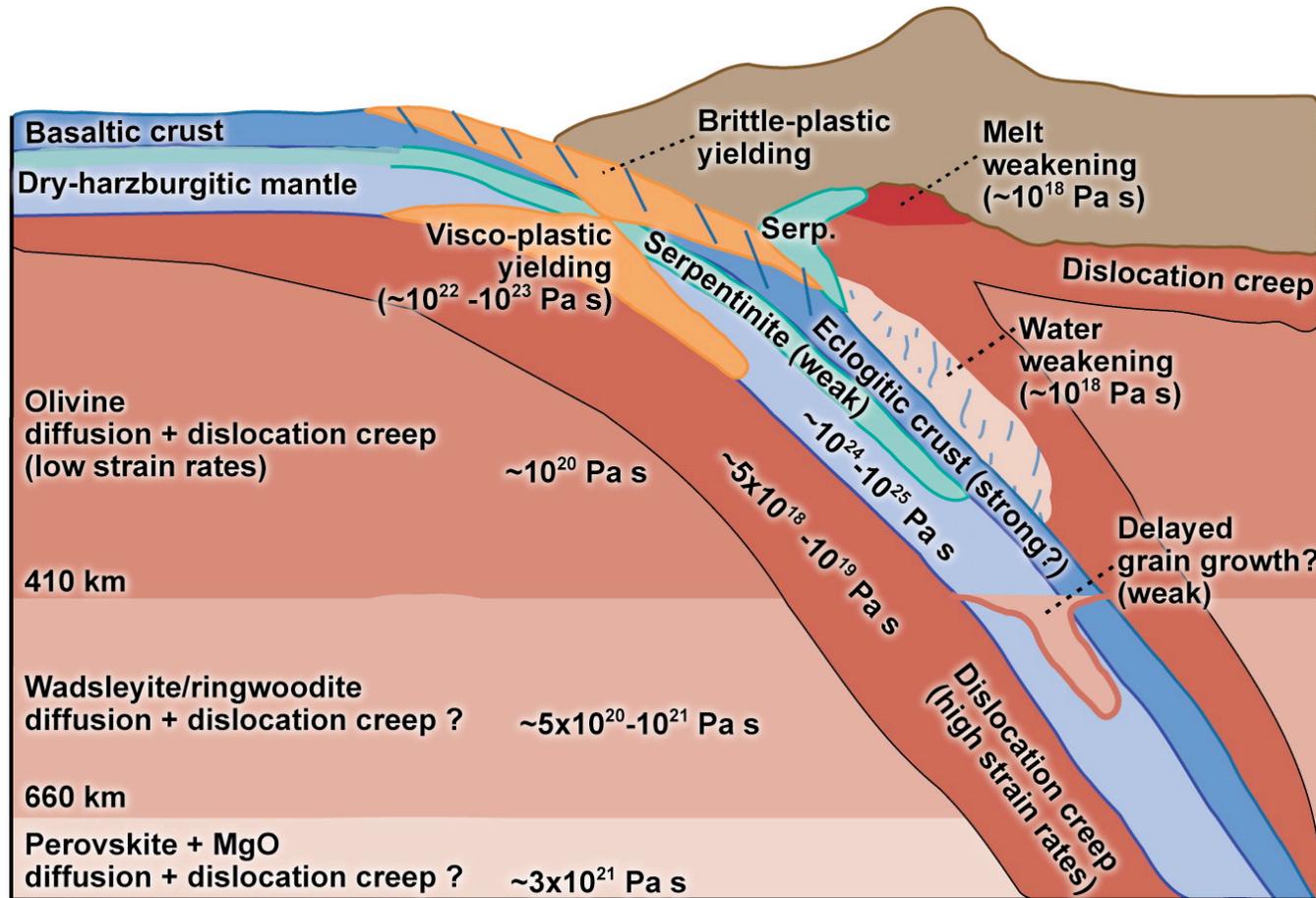
Material Properties: Density

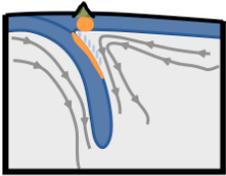


- **Previous, recent, models on**
 - *phase transitions, meta-stable olivine*
 - *mantle wedge dynamics*
 - *oceanic plateau subduction*
- **Lack of recent models evaluating**
 - *Local density variation in 3D (linked to composition).*



Material Properties: Rheology





Material Properties: Rheology

Laboratory experiments: large temperature, strain-rate & grain-size dependence.

- Viscous flow law (for each mechanism):

$$\eta = \left(\frac{d^p}{Ae^{(a\phi)}C_{OH}^r} \right)^{\frac{1}{n}} \dot{\epsilon}_{II}^{\frac{1-n}{n}} \exp \left[\frac{E + P_{lc}V}{nRT_t} \right]$$

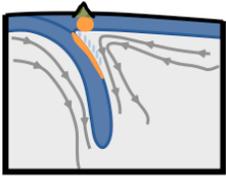
where,

$$T_t = T + T_{ad}.$$

P_{lc} is the lithostatic pressure, including a compressibility gradient.

For dislocation (ds) creep $p = 0$, $n = 3.5$.

For diffusion (df) creep $p = 3$, $n = 1$.



Material Properties: Rheology

- Dislocation (ds) & diffusion (df) creep accommodate total strain-rate:

$$\dot{\epsilon} = \dot{\epsilon}_{df} + \dot{\epsilon}_{ds} \quad (2)$$

- For deformation at constant stress, the effective viscosity is:

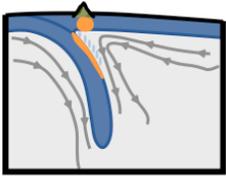
$$\eta_{ef} = \frac{\eta_{df}\eta_{ds}}{\eta_{df} + \eta_{ds}} \quad (3)$$

For a background upper mantle viscosity of $\eta_o = 10^{20}$ Pas (at 250 km):

– Transition strain-rate ($\dot{\epsilon}_{df} = \dot{\epsilon}_{ds}$): $\dot{\epsilon}_t = 10^{-15} \text{ s}^{-1}$

for $C_{OH} = 300$ ppm-H/Si & $d = 10$ mm.

Dislocation creep decreases viscosity where the strain-rate is more than the transition value.



Material Properties: Rheology

- Plastic yield stress, σ_y , limits the stress (and viscosity).

If,

$$\sigma_y > \eta_{df} \dot{\epsilon}_{II}$$

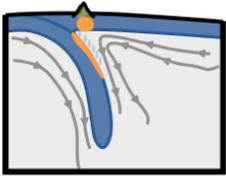
then,

$$\eta_y = \sigma_y / \dot{\epsilon}_{II}$$

- Composite viscosity:

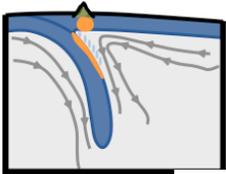
$$\eta_{comp} = \min(\eta_{ef}, \eta_y)$$

- ***Non-deforming regions remain highly viscous.***
- ***Yielding concentrates deformation.***

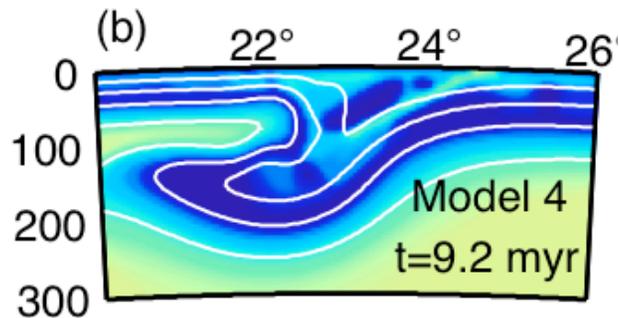
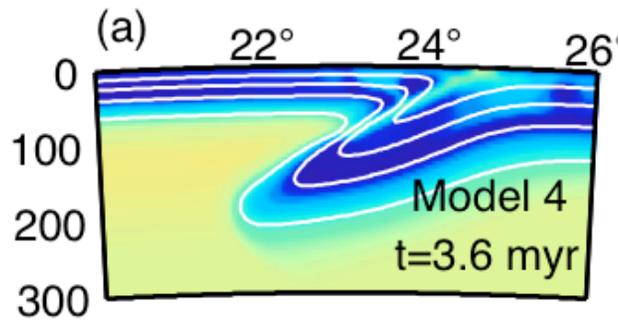


Rheology: Examples

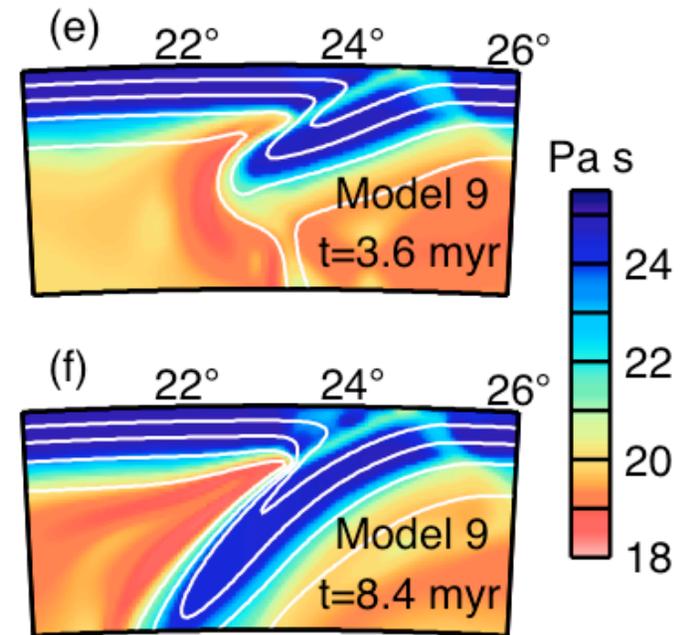
- *Subduction initiation*
- *Long term subduction*
- *3D instantaneous flow*
 - *Margarete Jadamec (PhD 2009)*
- *Ridge-trench interaction*
 - *Erin Burkett (PhD, exp. 2010)*



1. 2D Subduction Initiation

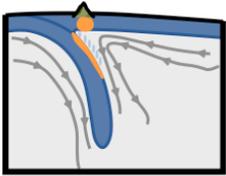


Newtonian

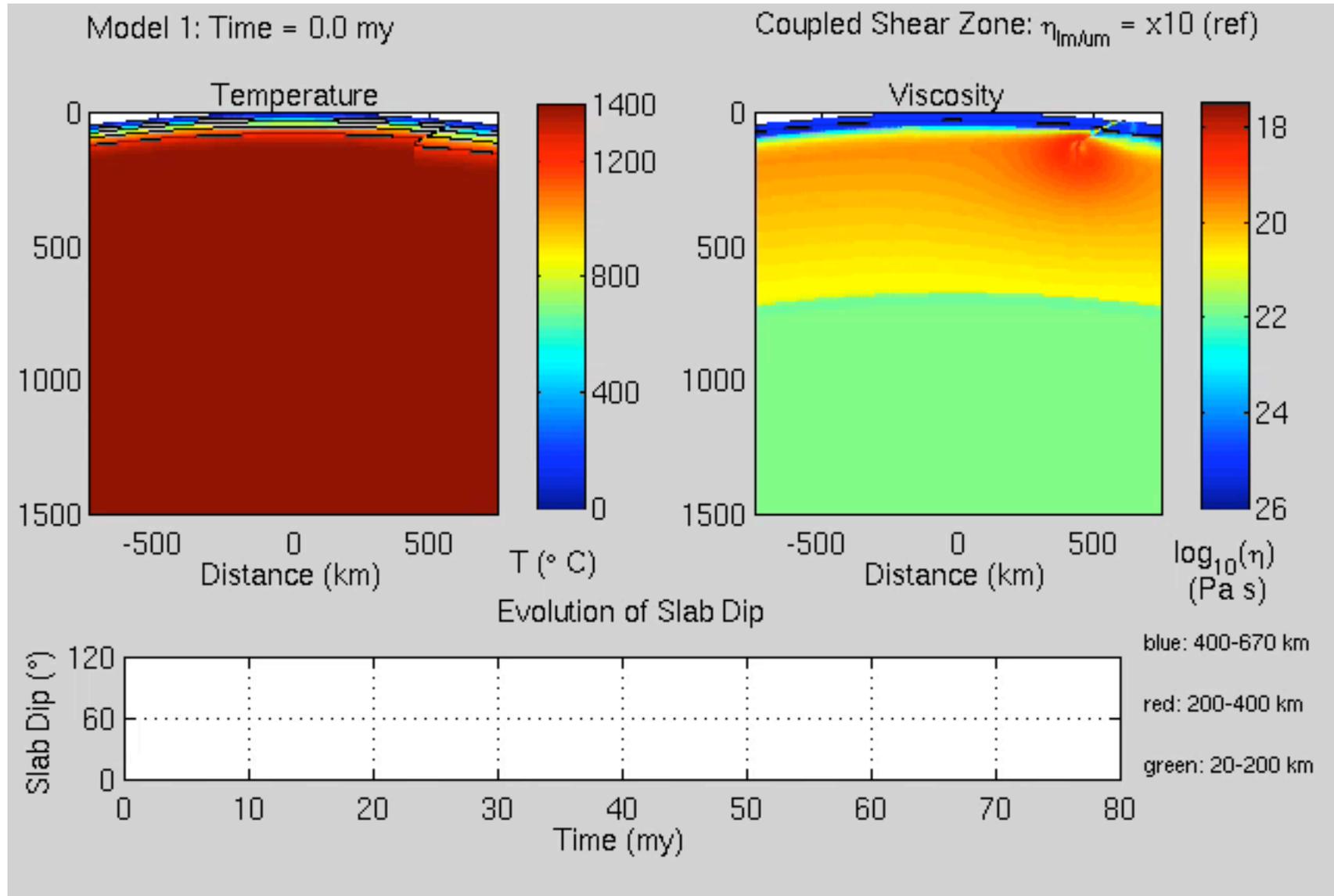


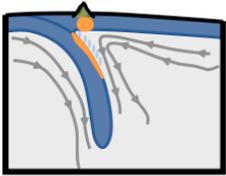
Composity Viscosity

- *Strain-rate weakening can counteract temperature-dependent strengthening.*

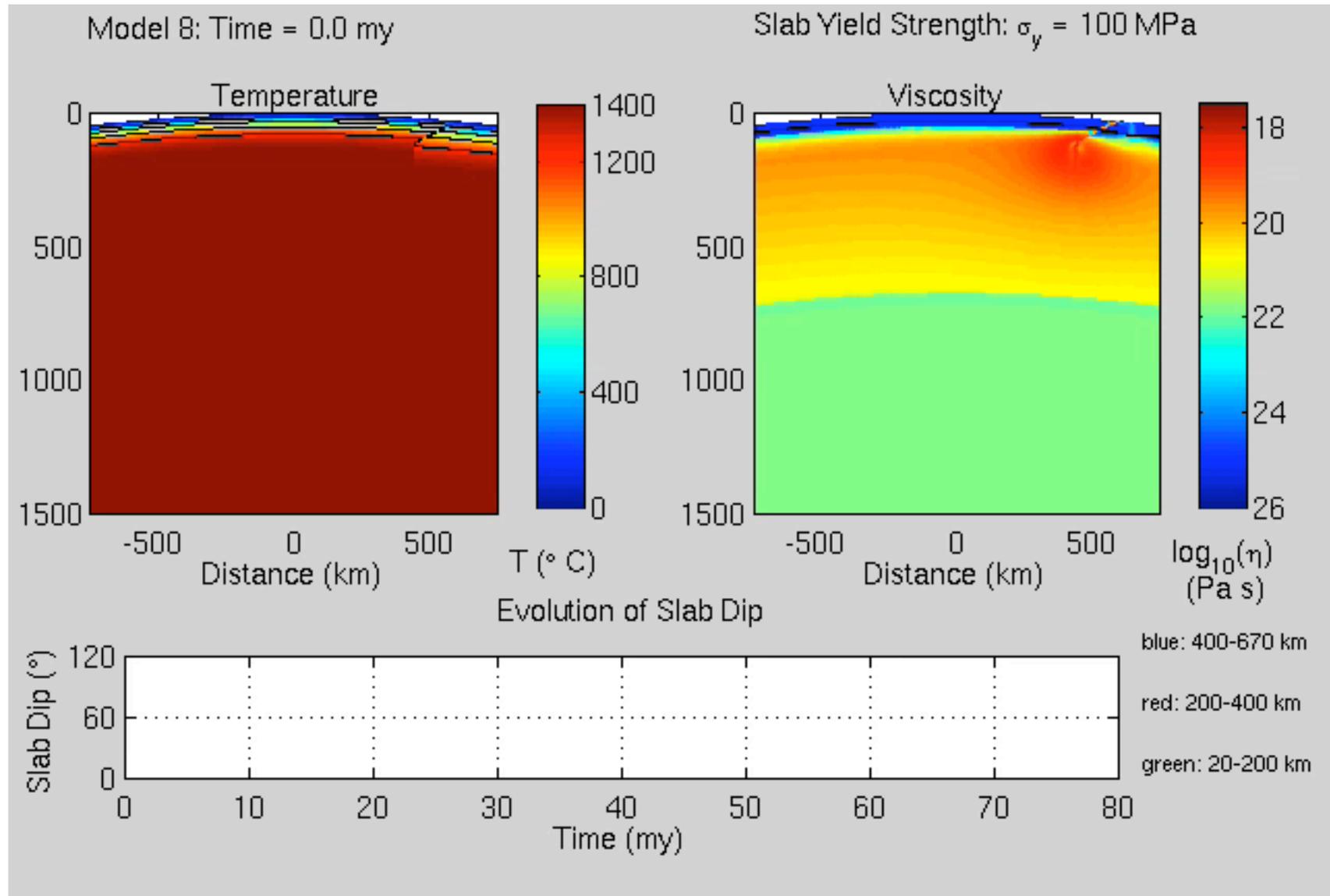


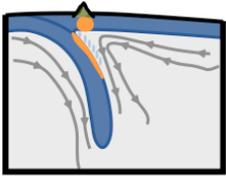
2. 2D Long Term Subduction



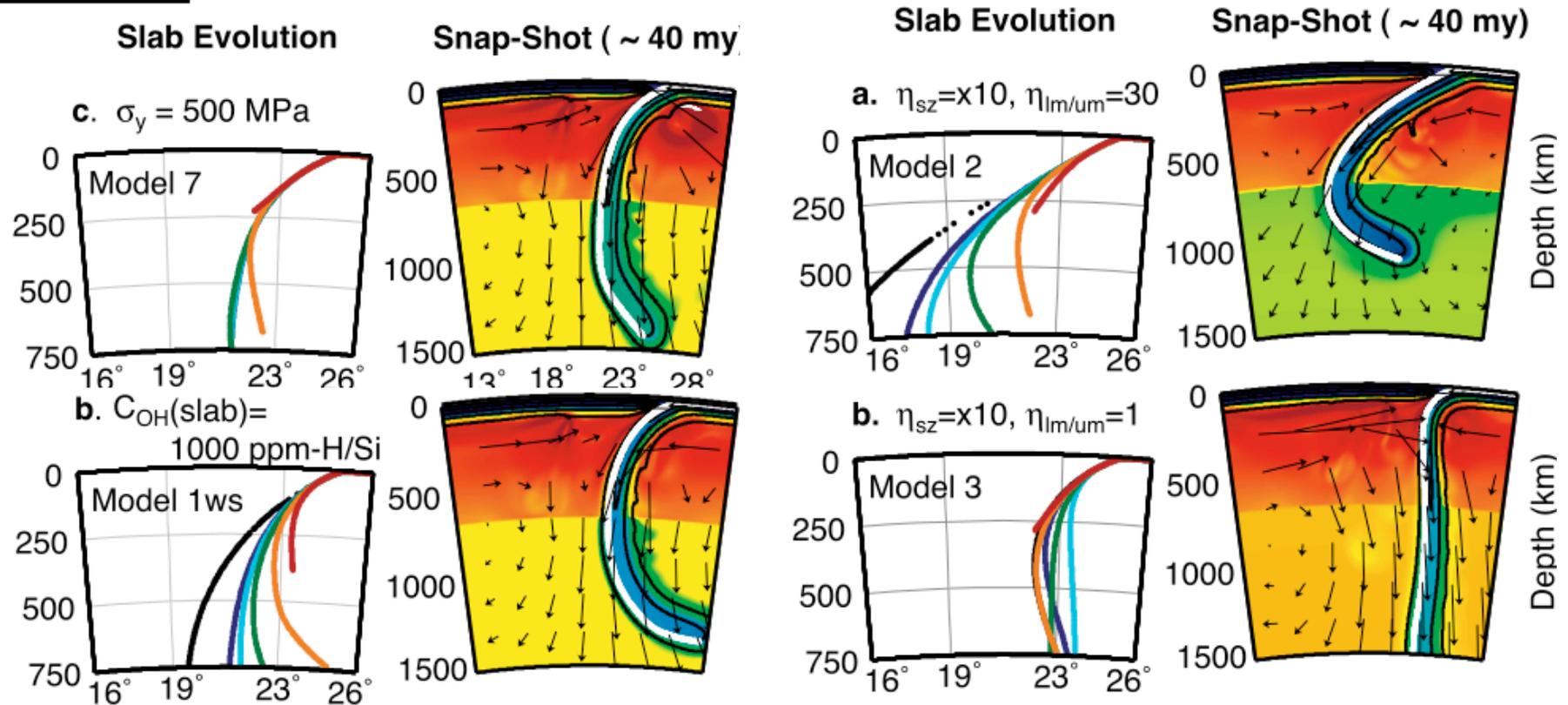


2. 2D Long Term Subduction

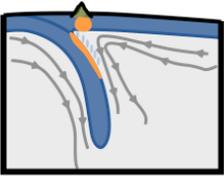




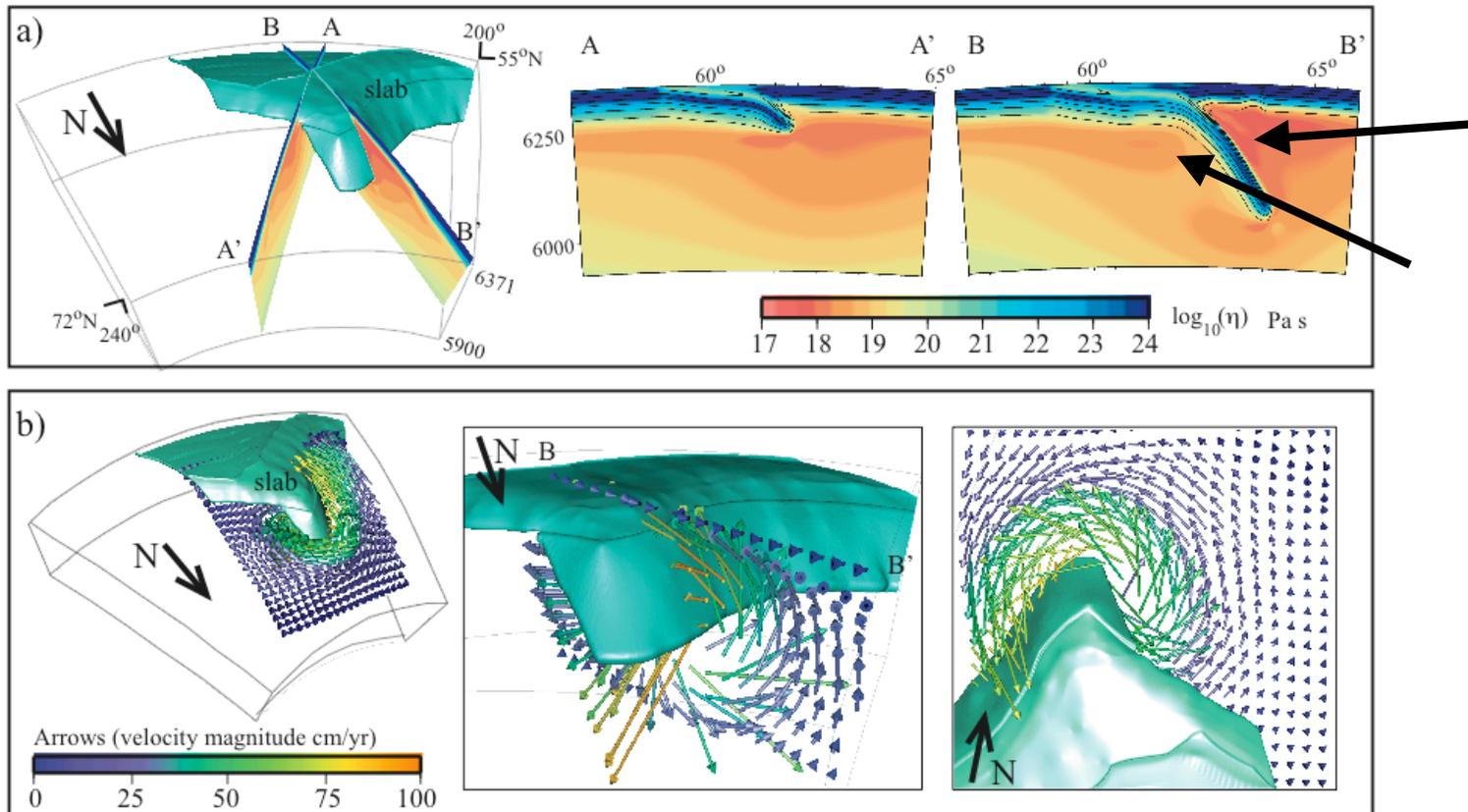
2. 2D Long Term Subduction



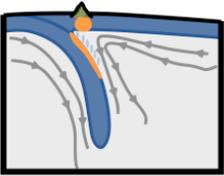
- **High yield stress allows slab to:**
 - Better support own weight; Transfer stress along slab
 - But depends on lower mantle viscosity



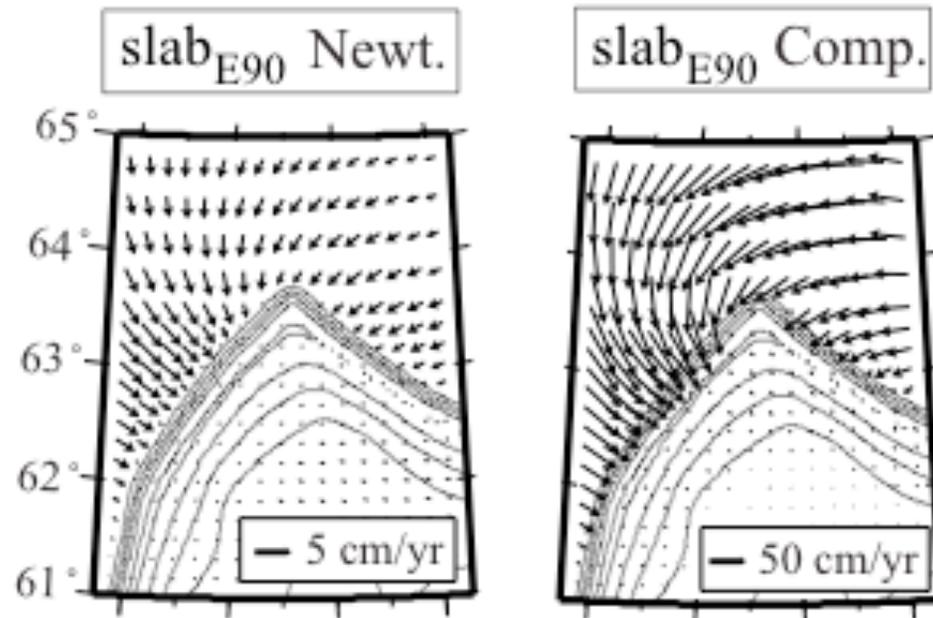
3. 3D Flow at a Slab Edge



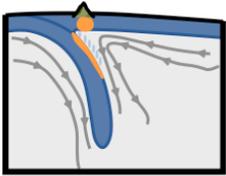
- **Strain-rate weakened region provides little viscous support for upper-mantle slab.**
 - Slab is steepening (transient state of UM slabs?)
 - Strong coupling between toroidal and poloidal flow.



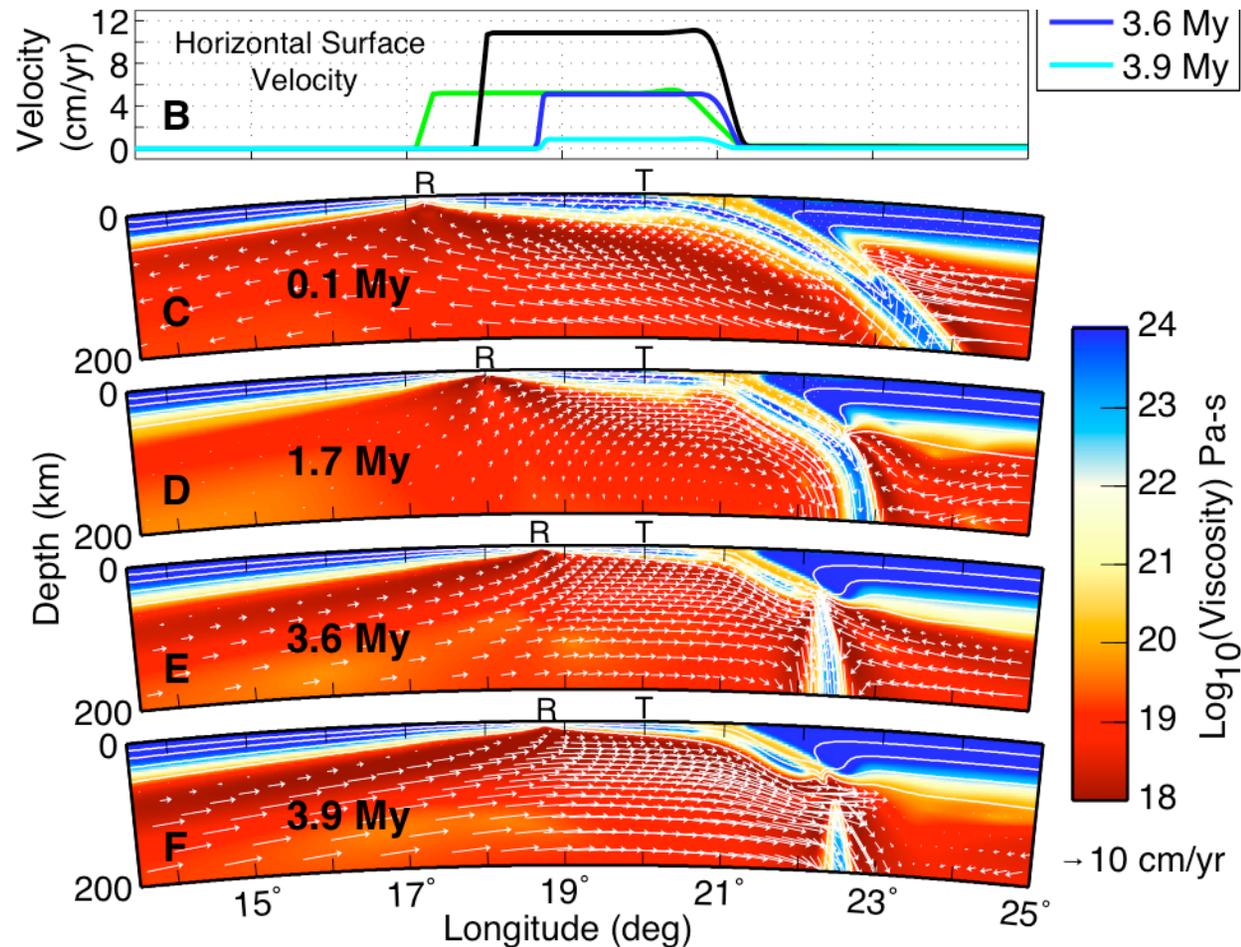
3. 3D Flow at a Slab Edge



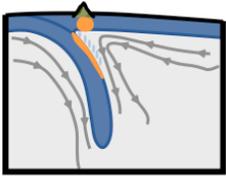
- ***Newtonian vs non-Newtonian flow:***
 - *Similar pattern, but stronger toroidal component.*
 - *Flow rate is 10-80 times faster.*
 - *Decouples surface plates from mantle flow (transient?)*



4. Ridge-Trench Interaction

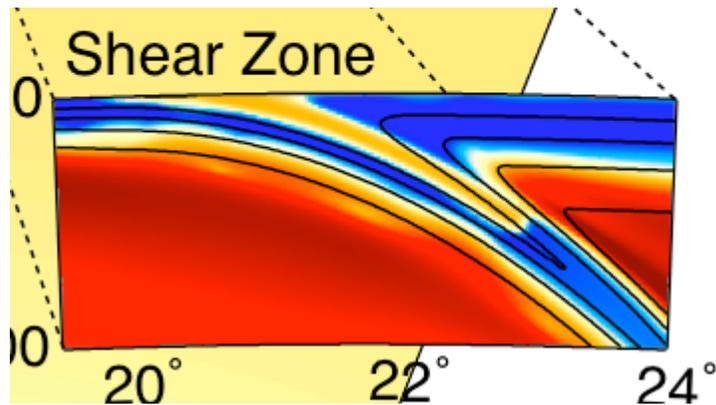
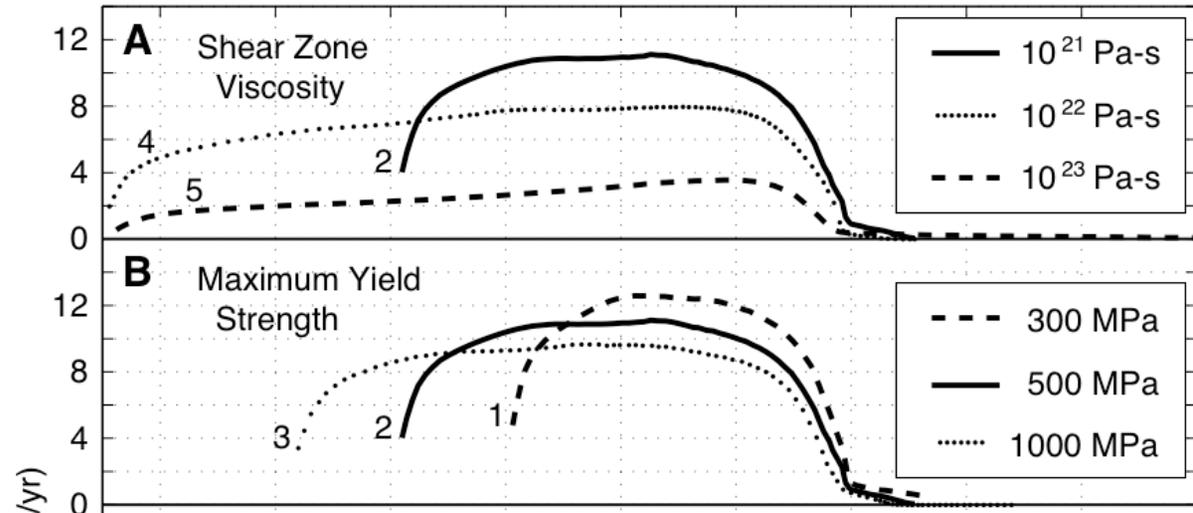


- *High yield stress & non-Newtonian viscosity leads to plate-like motion of young lithosphere.*

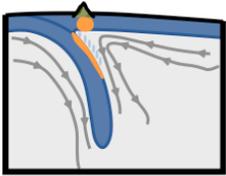


4. Ridge-Trench Interaction

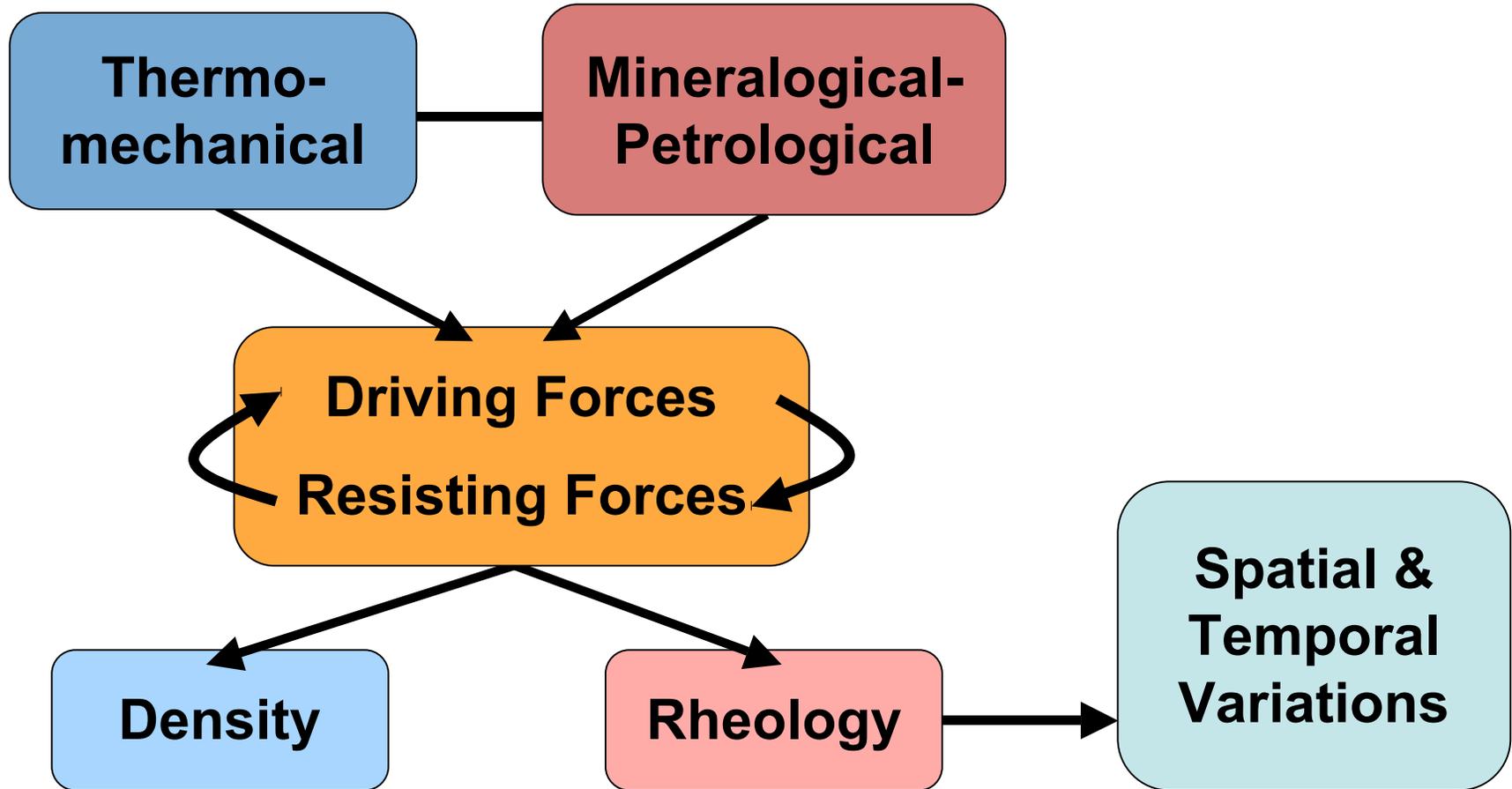
- *Yielding within slab leads to slab detachment before ridge subduction.*

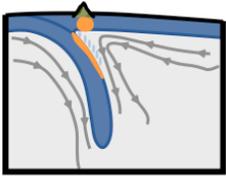


- *Young plates have insufficient slab-pull to drive subduction in Newtonian mantle.*

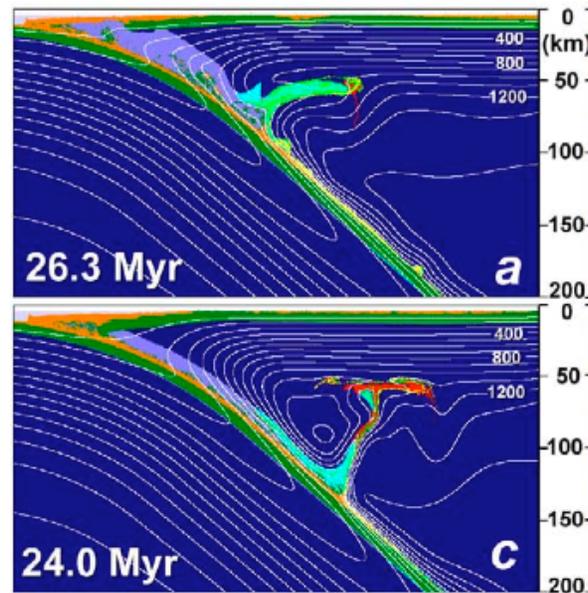
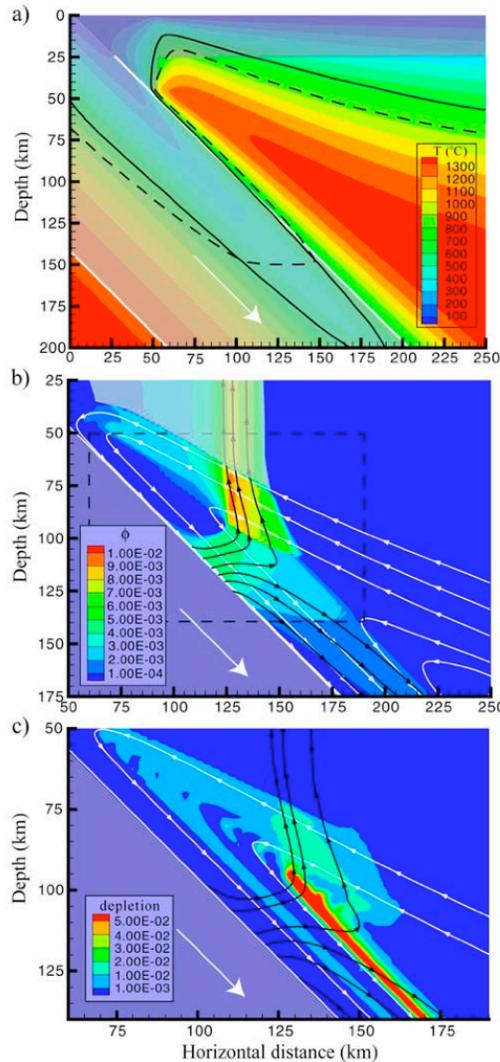


The Dynamical System





Mineralogical-Petrological



Fully-coupled mantle-wedge dynamics & petrology

- Baker-Hebert et al., 2009

Fluid transport, melting

- Cagniole et al., 2007

Composite crust-mantle density & rheology in wedge

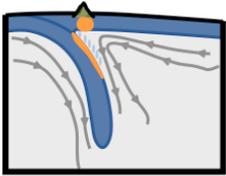
- Gerya & Yuen, 2003

Min./pet. implications

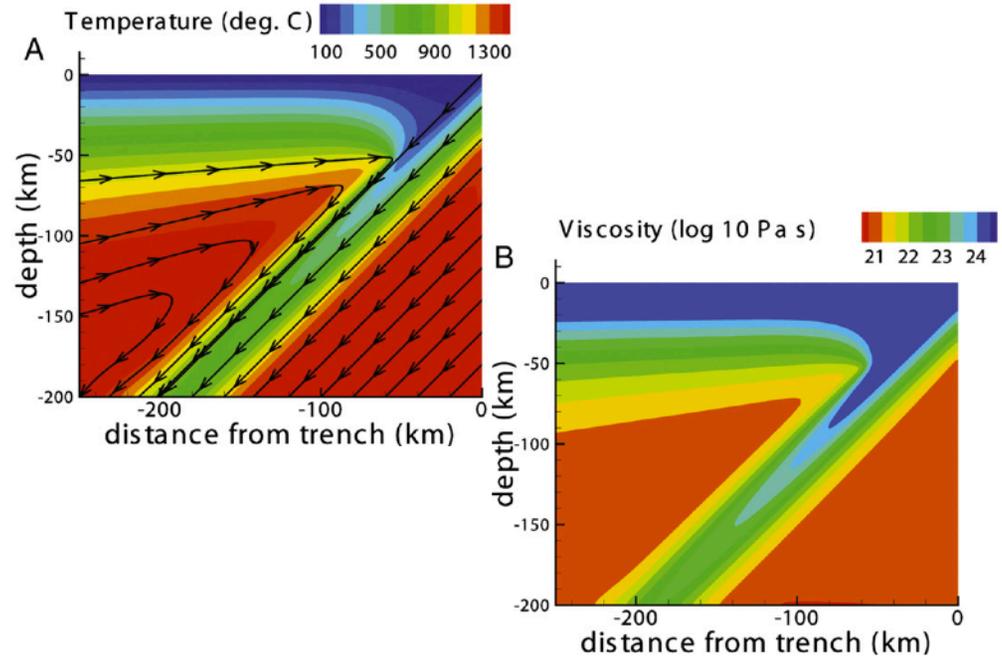
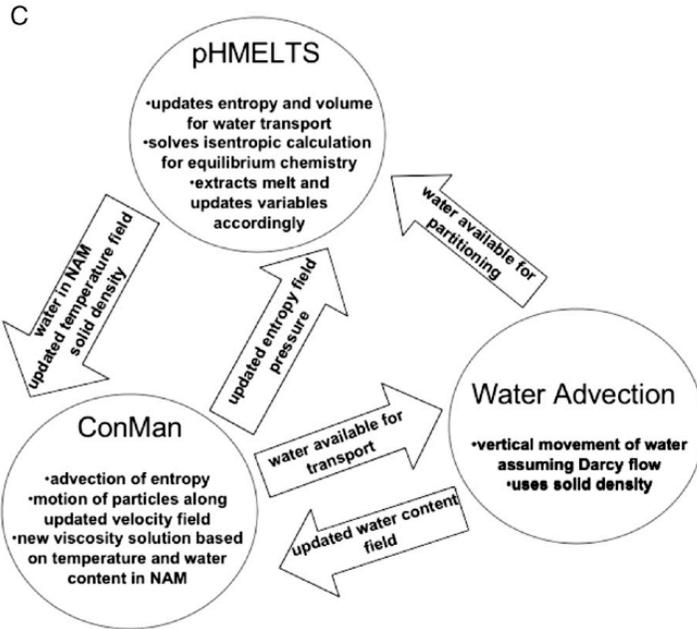
- Davies & Stevenson, 1992

1990s → 2000s

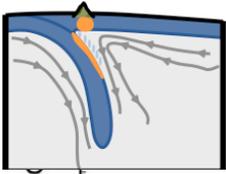
- *Need coupled solid & fluid flow, density & rheology, detailed tracking of composition & phase.*



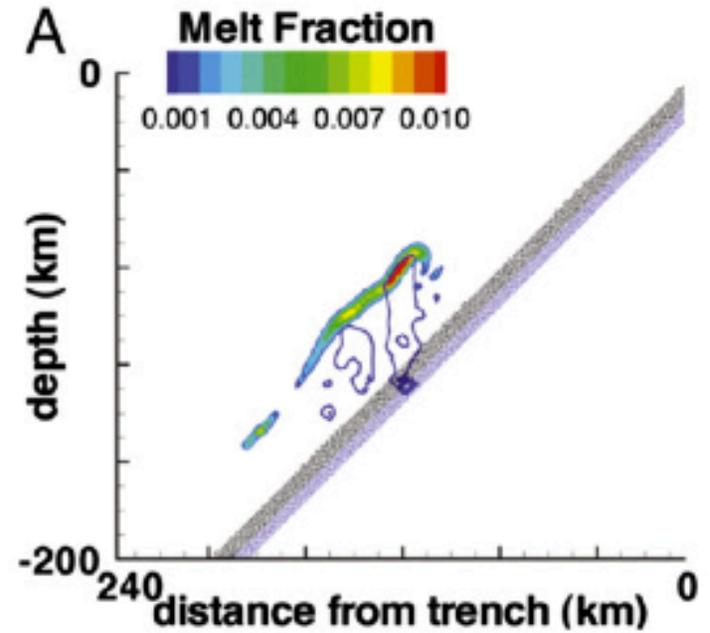
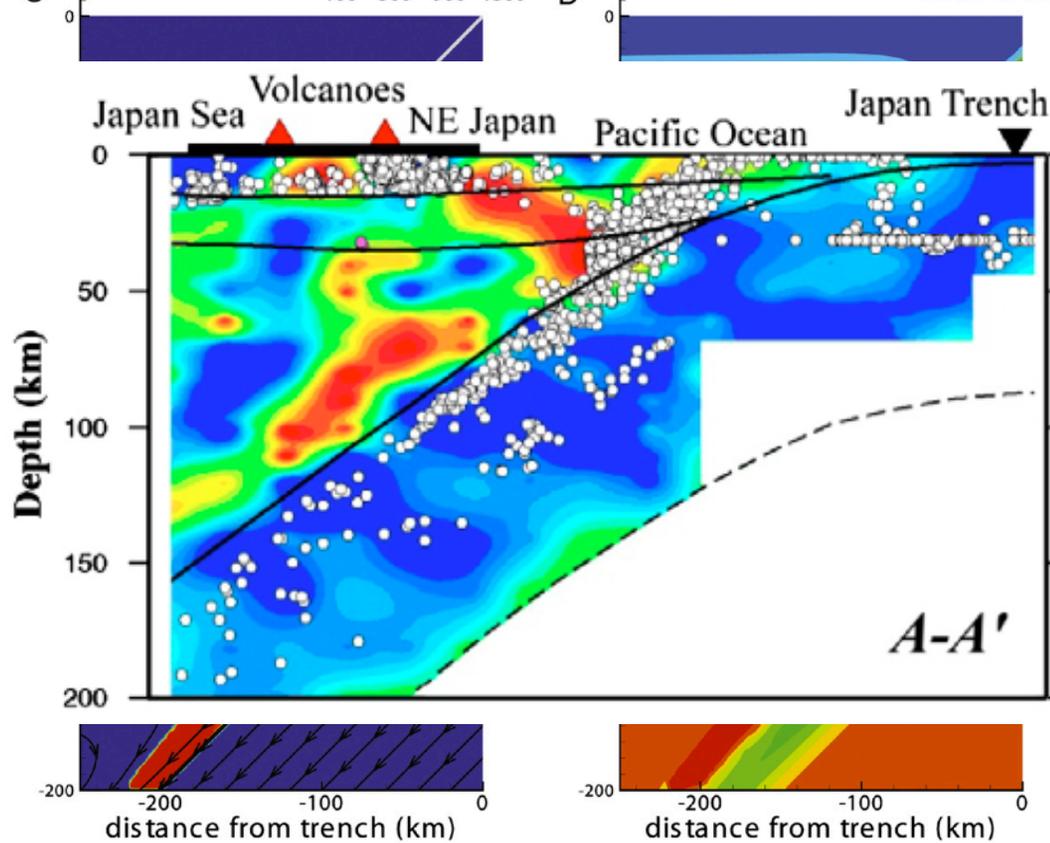
Coupled Solid-Fluid-Min.



- Composition evolves including fluid & melt content.
 - Affects density (T, X) & rheology.
- Fluids move according to Darcy flow

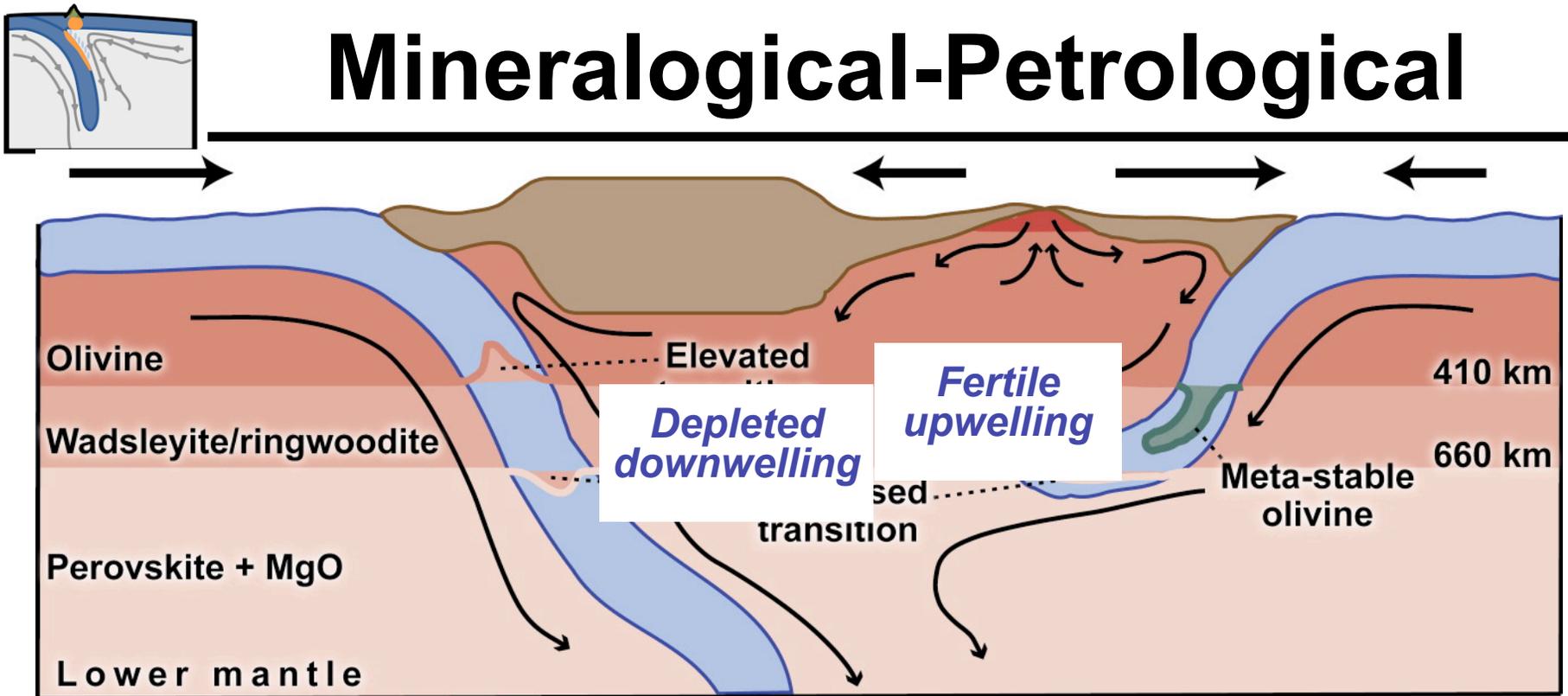


Fluids Affect Solid Flow.

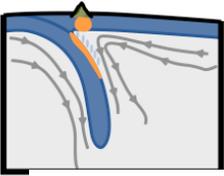


- *Form low viscosity channel above slab.*
- *Spatially & temporally variable melt fraction.*
 - *Limits region of water effect on rheology.*

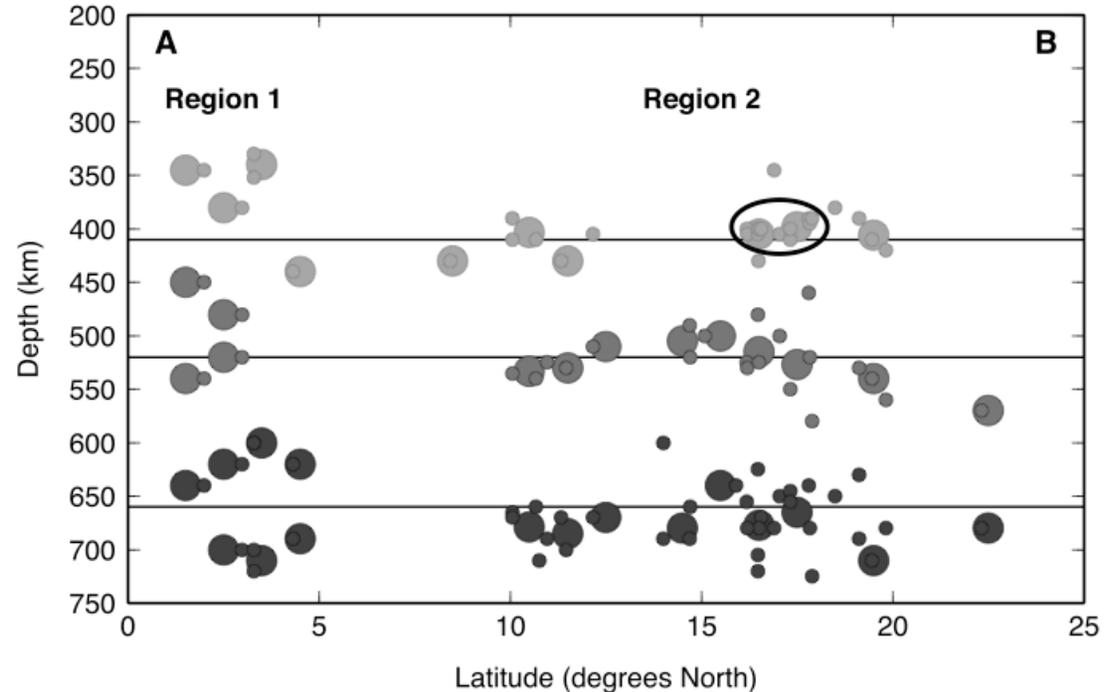
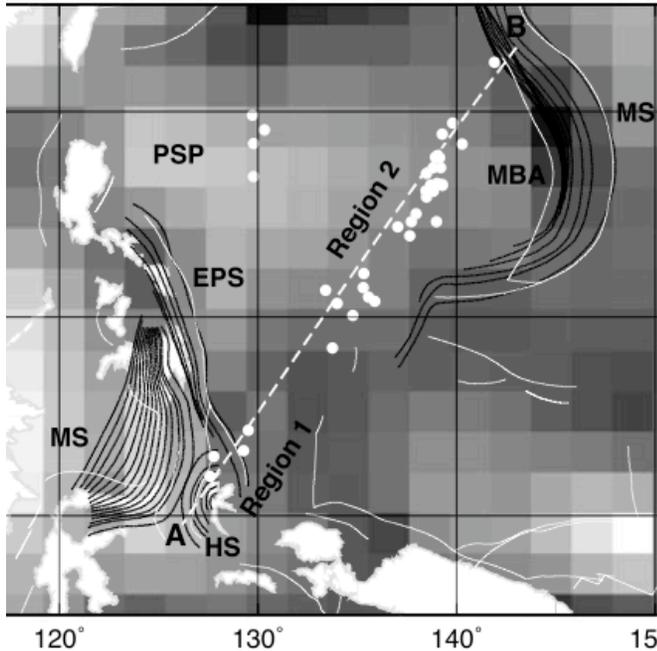
Mineralogical-Petrological



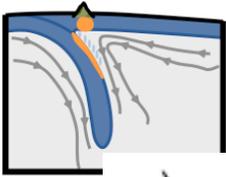
- ***Expect compositional variation in the transition zone due to shallow mantle processes.***
 - ***Density variations (Fe content, major ele. depletion)***
 - ***Rheological variations (OH, grain growth & pinning)***



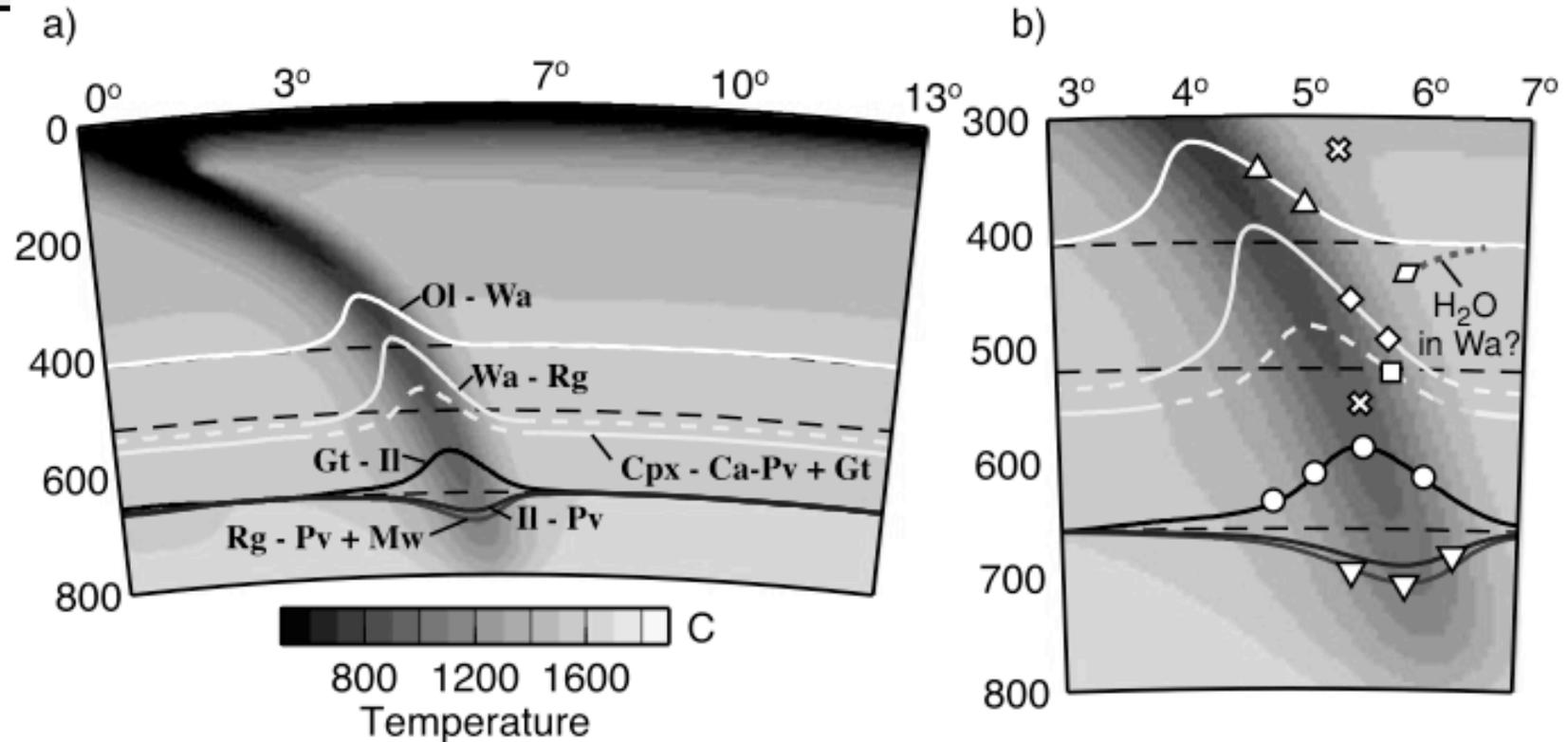
Mid-mantle Seismic Reflectors



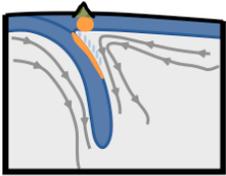
- *Slab region: Shallow & deep 410 km (?), 520- km reflector, paired 660-km reflectors*
- *Non-slab region: Hint of structure on 520-km reflector, 410 & 660 are confusing?*



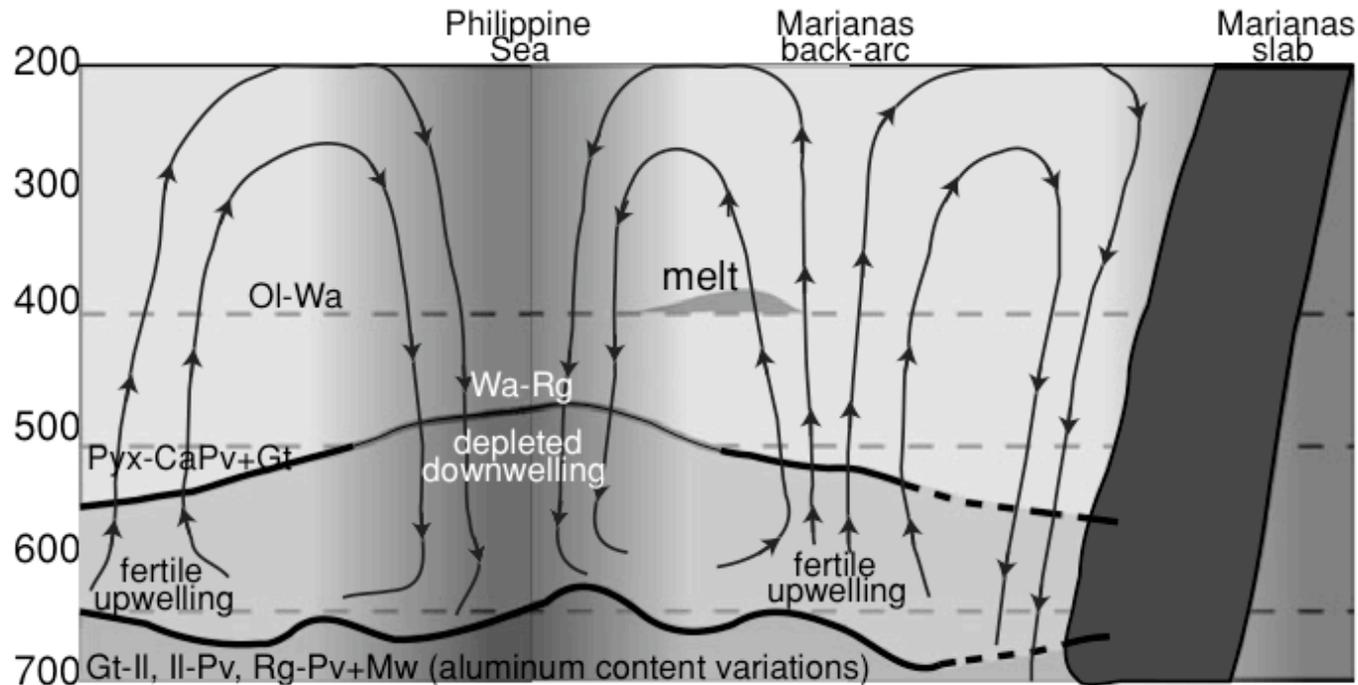
Mineralogical-Petrological



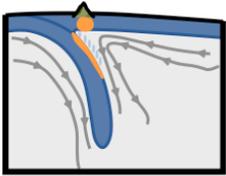
- **Laboratory data & dynamical models**
– **Can see non-olivine component in slabs**



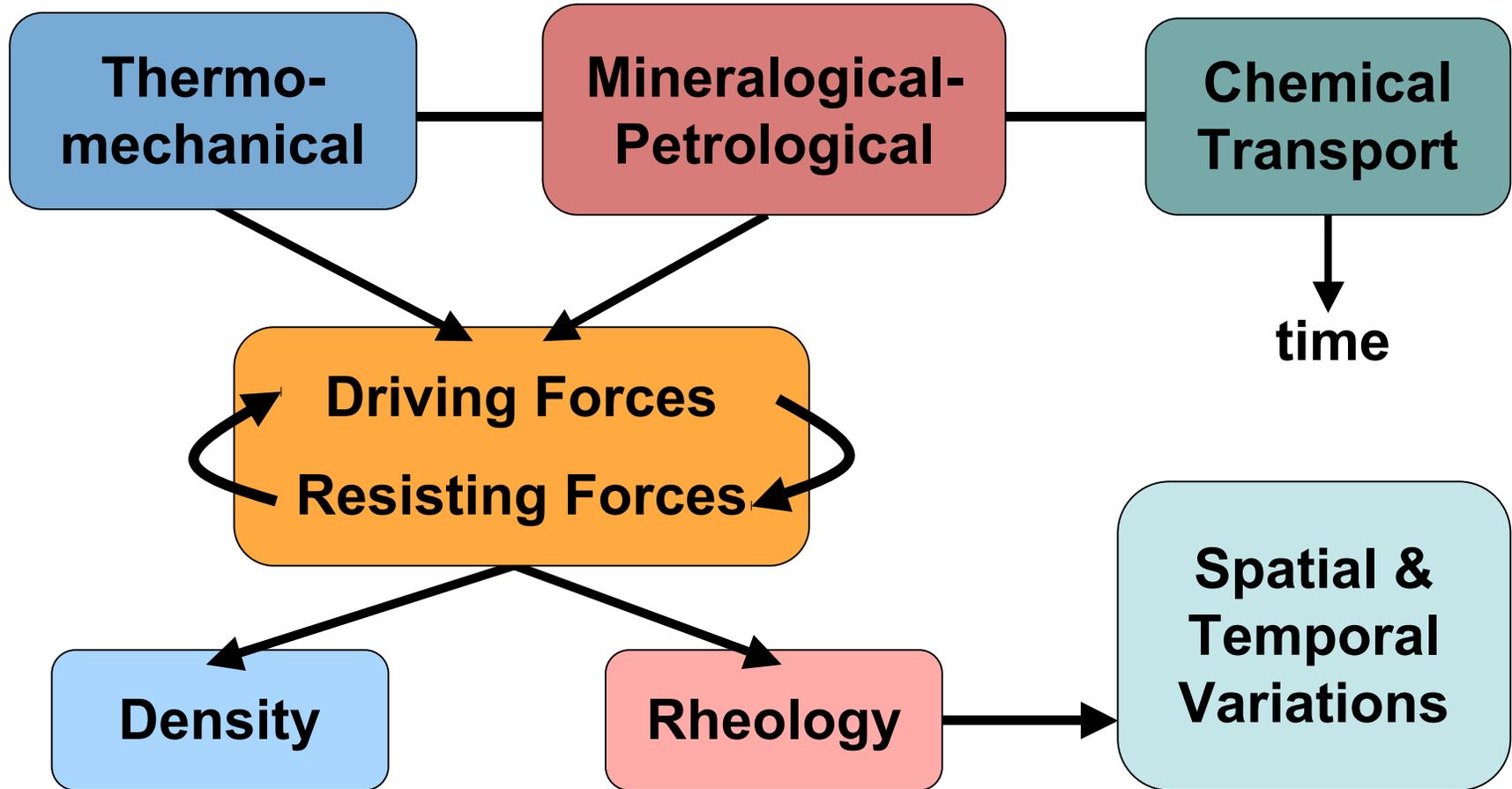
Mineralogical-Petrological

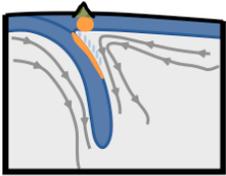


- ***Other variations can be interpreted in terms of surface tectonics & shallow mantle processes.***
 - ***Fertile upwelling (return flow from subduction)***
 - ***Depleted downwelling below back-arc spreading.***

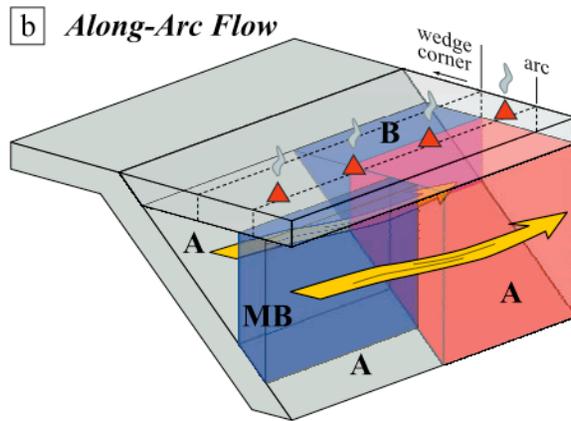
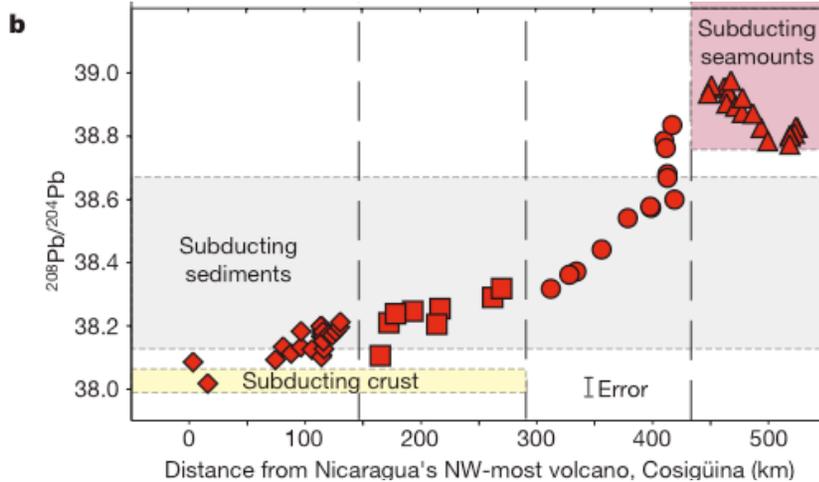


The Dynamical System

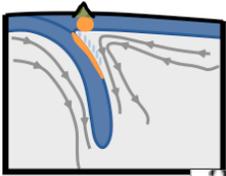




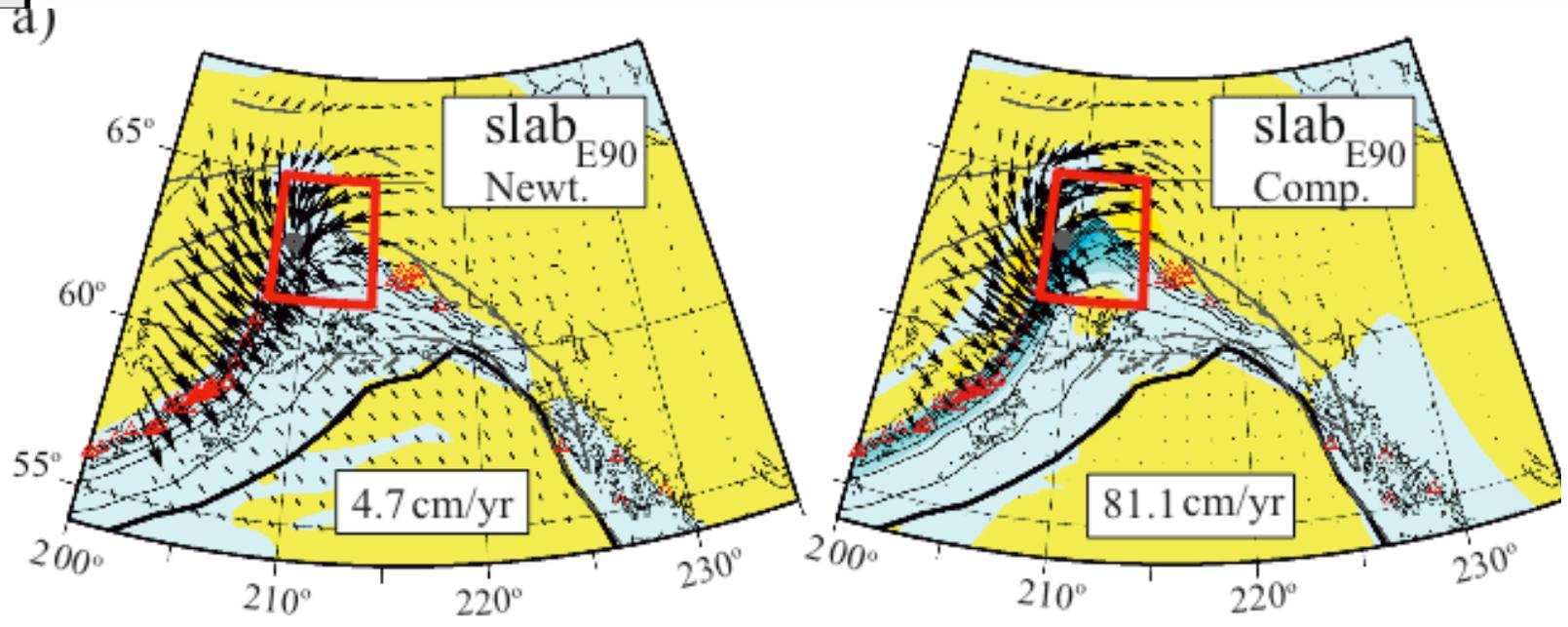
Chemistry Transport



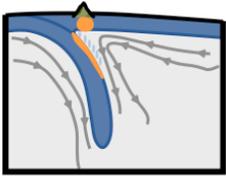
- **Fast Rates:**
 - > 16 cm of trench-parallel flow
 - 2 x as fast as sub. plate rate.
 - Implies even faster poloidal flow.
 - Decoupling of surface plate & mantle flow.
- **Constraint on solid flow velocity**
 - Constraint on magnitude of viscosity.



Chemical Transport

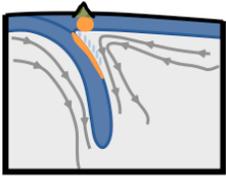


- **3D model of Alaska (non-Newtonian) leads to decoupling & fast mantle flow rates, but...**
 - Don't get strong component of along-strike flow (different geometry?)

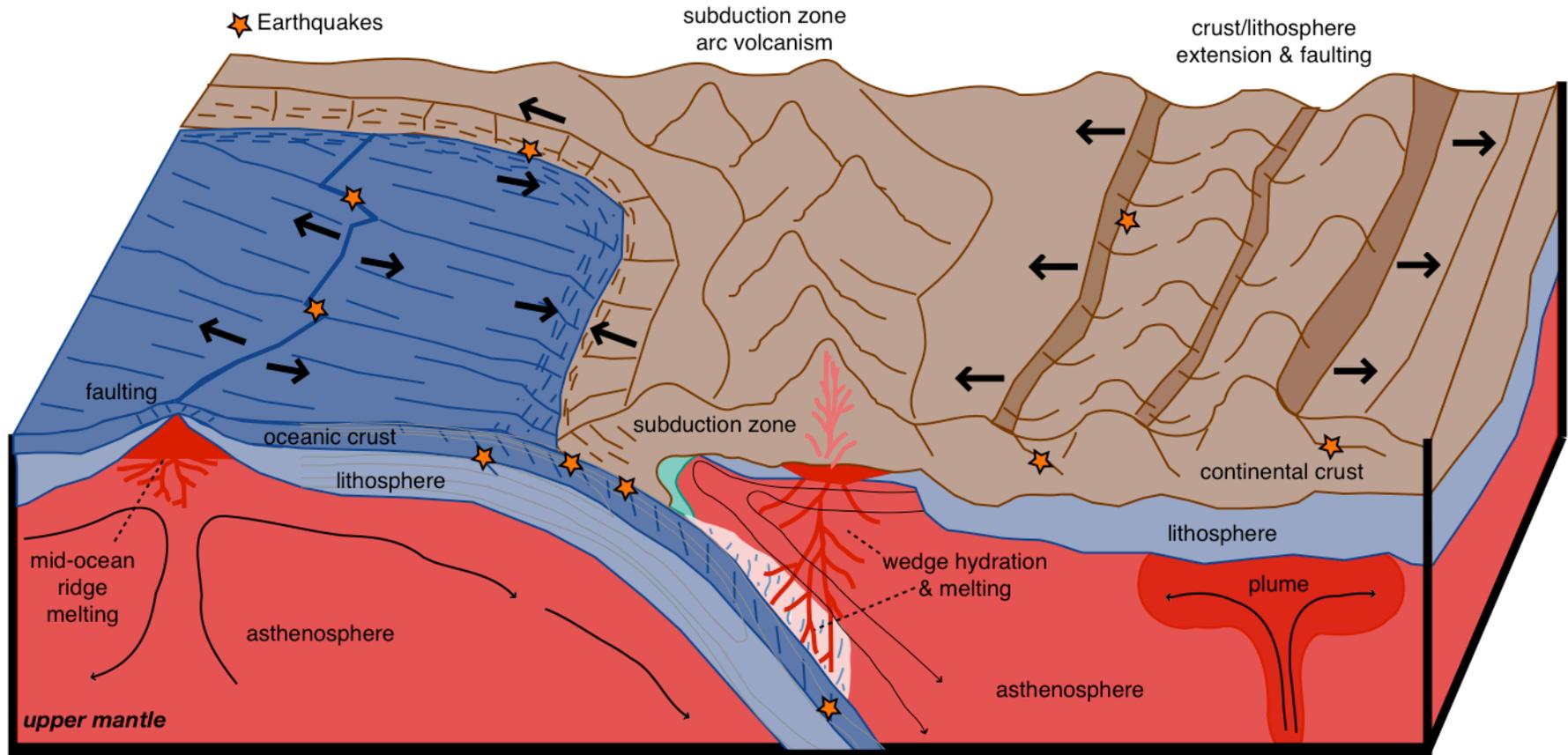


Conclusions

- ***Modeling of subduction dynamics is benefiting from,***
 - ***Access*** to new & more complete observations.
 - ***Advances*** in numerical & analogue methods.
 - ***Ability*** to link dynamics to other disciplines.
- ***New models are beginning to show how multi-processes are linked.***
- ***New results will challenge our standard view of mantle-plate coupling (flow patterns, flow rates).***



Conclusions



Using multiple observations to understand dynamics is key to determining what processes are important for a dynamic theory of plate tectonics.